

The 2016 Atomic Mass Evaluation and the Mass Tables

Georges Audi

Csnsn

September 2016

the future of the Ame & Nubase evaluations

last published Tables : December 2012 in CPC

now at IMP-Lanzhou : WANG Meng (王猛) new coordinator

next publication planned : December 2016

the Atomic Mass Evaluation (AME)

the experimental data

data evaluation - data treatment - adjusted masses

regularity - estimated unknown masses



原子质量评估备忘录签字仪式

Memorandum Signing Ceremony
Atomic Mass Evaluation



The new AME collaboration

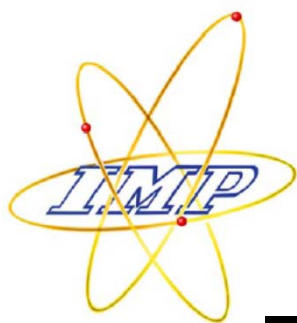
Coordinator

Meng Wang^a

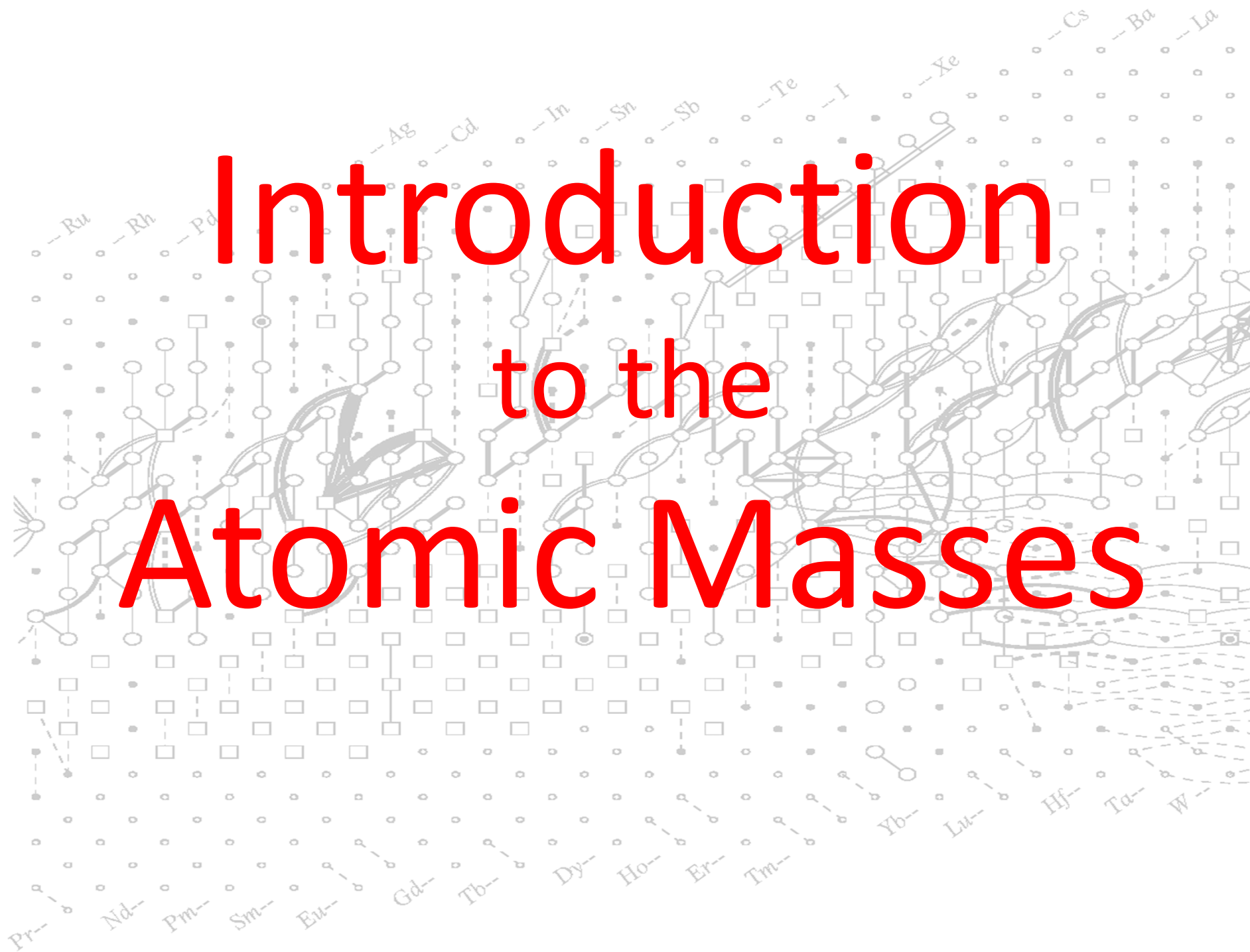
Contributors

Georges Audi^b, Wenjia Huang^b, Filip Kondev^c, Sarah Naimi^d

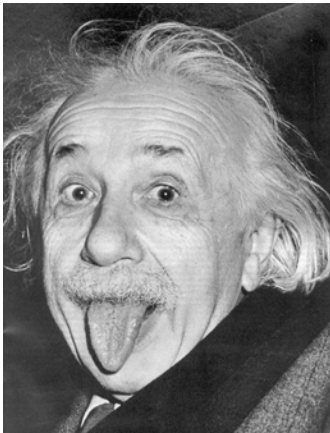
a.IMP-Lanzhou b.CSNSM-Orsay c.ANL-Argonne d.RIKEN



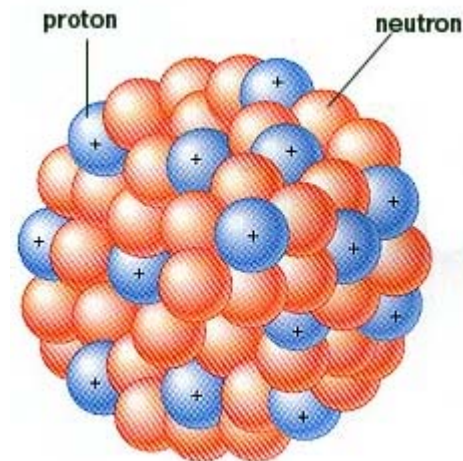
Introduction to the Atomic Masses



Atomic mass

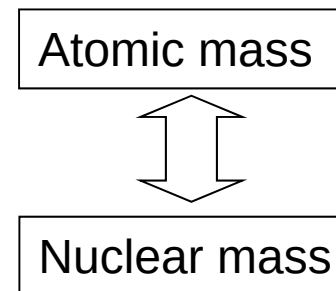


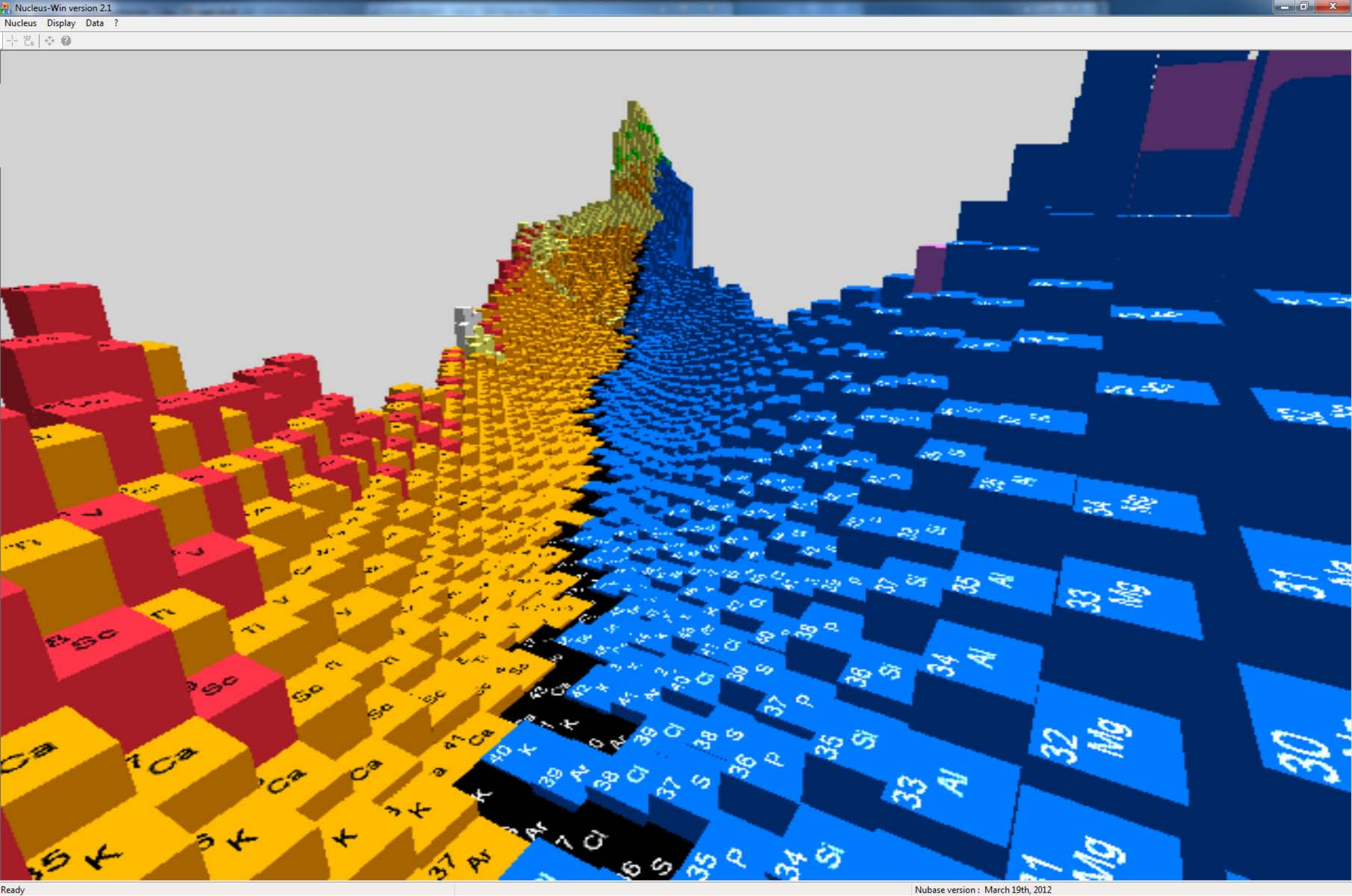
$$E = mc^2$$



Nuclear physics
Atomic physics
Nuclear astrophysics
Atomic energy
Fundamental symmetries
Metrology

.....



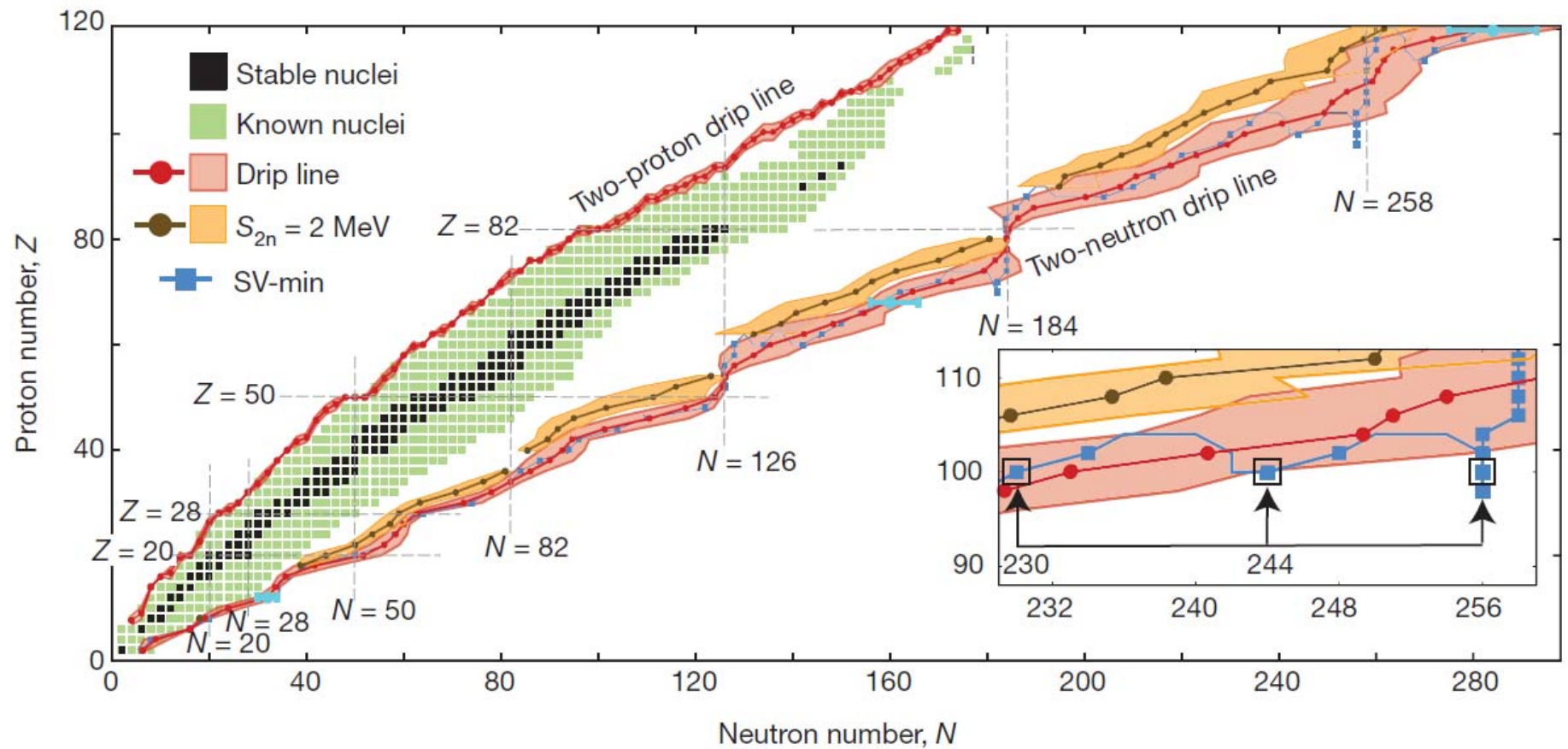


Exotic nuclei

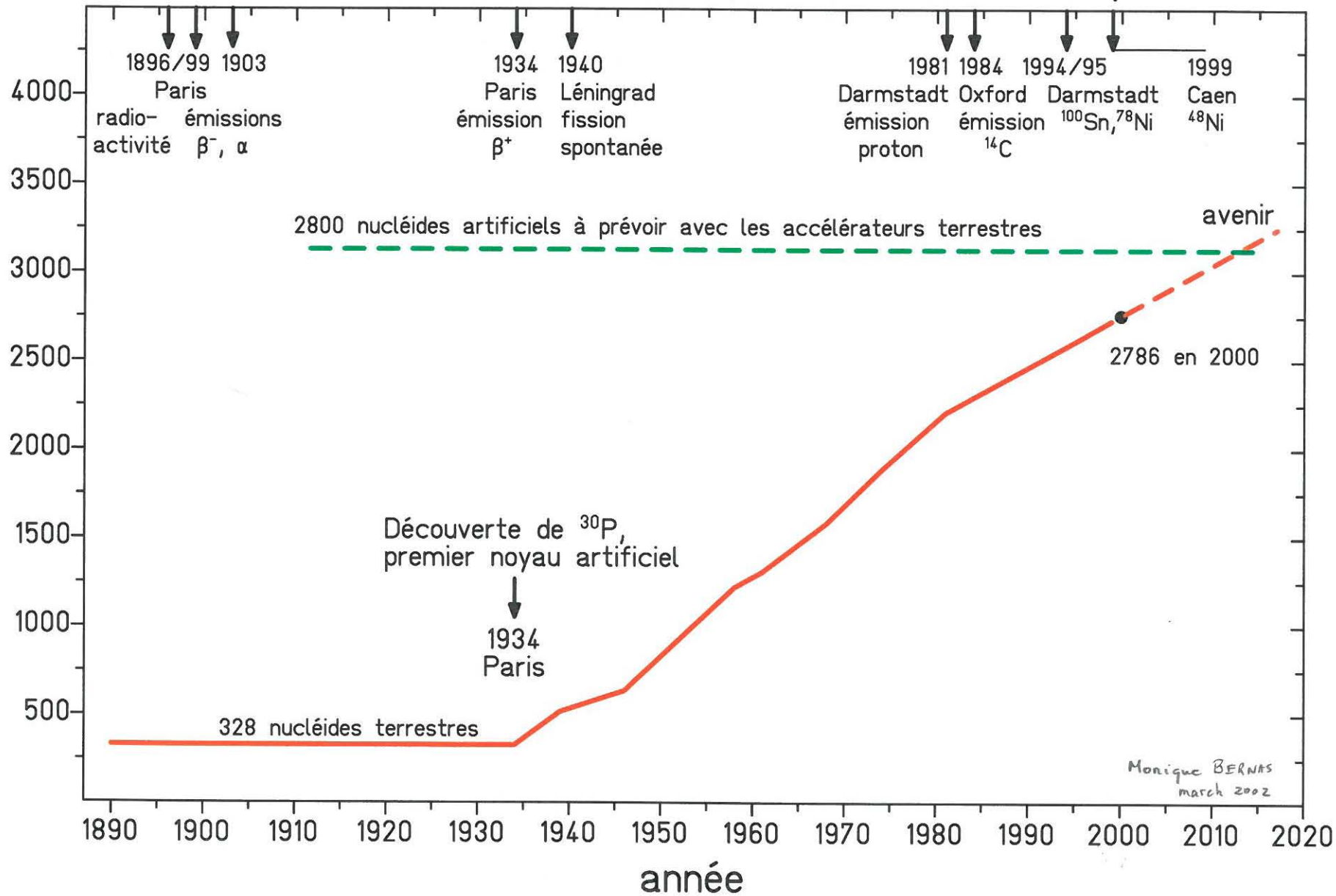
The limits of the nuclear landscape

doi:10.1038/nature11188

Jochen Erler^{1,2}, Noah Birge¹, Markus Kortelainen^{1,2,3}, Witold Nazarewicz^{1,2,4}, Erik Olsen^{1,2}, Alexander M. Perhac¹ & Mario Stoitsov^{1,2,†}



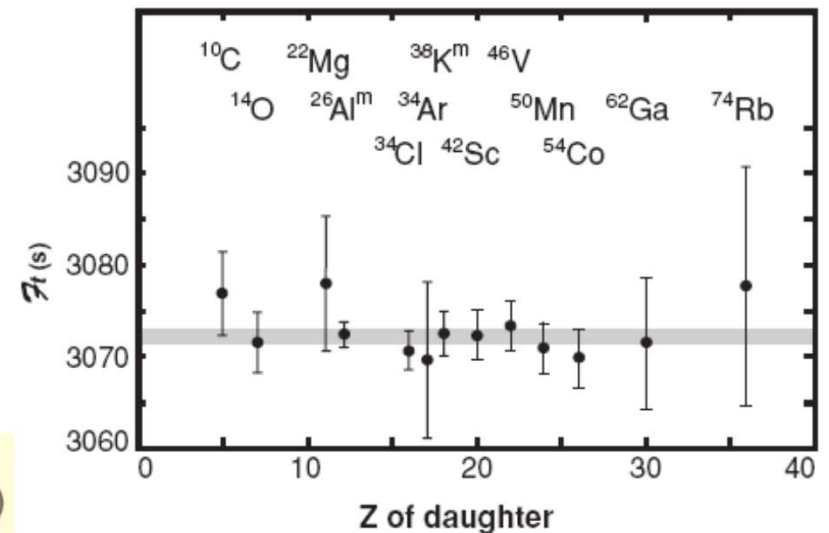
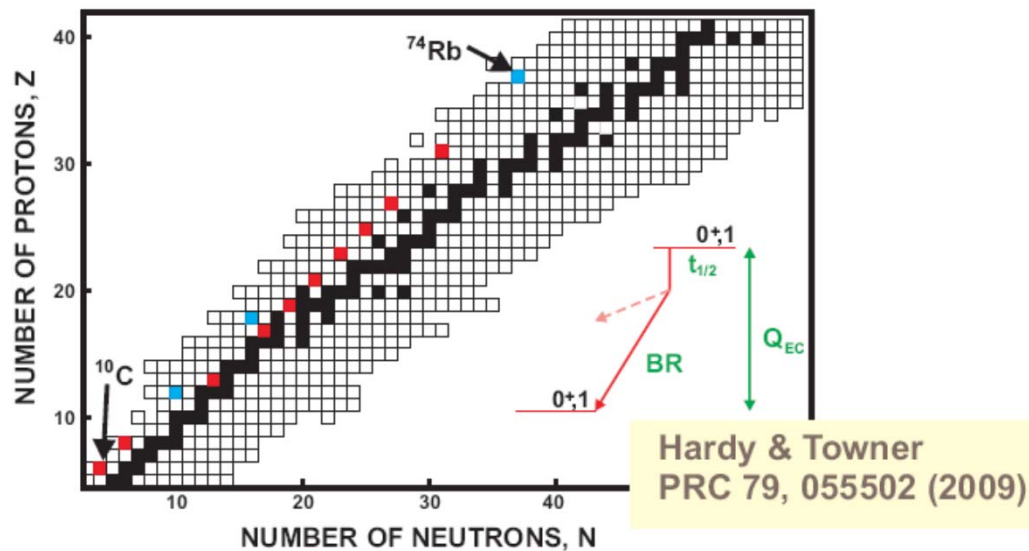
nombre des noyaux connus



Motivations

- Nuclear Physics
- Standard Model
- Neutrino Physics
- Astrophysics
- Atomic Physics

Superaligned $0^+ \rightarrow 0^+$ nuclear β decays



$$\mathcal{F}t = \frac{K}{2G_V^2(1 + \Delta_R^V)}$$

- **Test of**
the conserved vector current (CVC) hypothesis
- **Test of**
the unitarity of the Cabibbo-Kobayashi-Maskawa (CKM) matrix

1) G_V constant ✓ verified to $\pm 0.013\%$

2) $|V_{ud}| = G_V/G_\mu = 0.97425 \pm 0.00022$

3) CKM unitarity established ✓

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 0.99990 \pm 0.00060$$

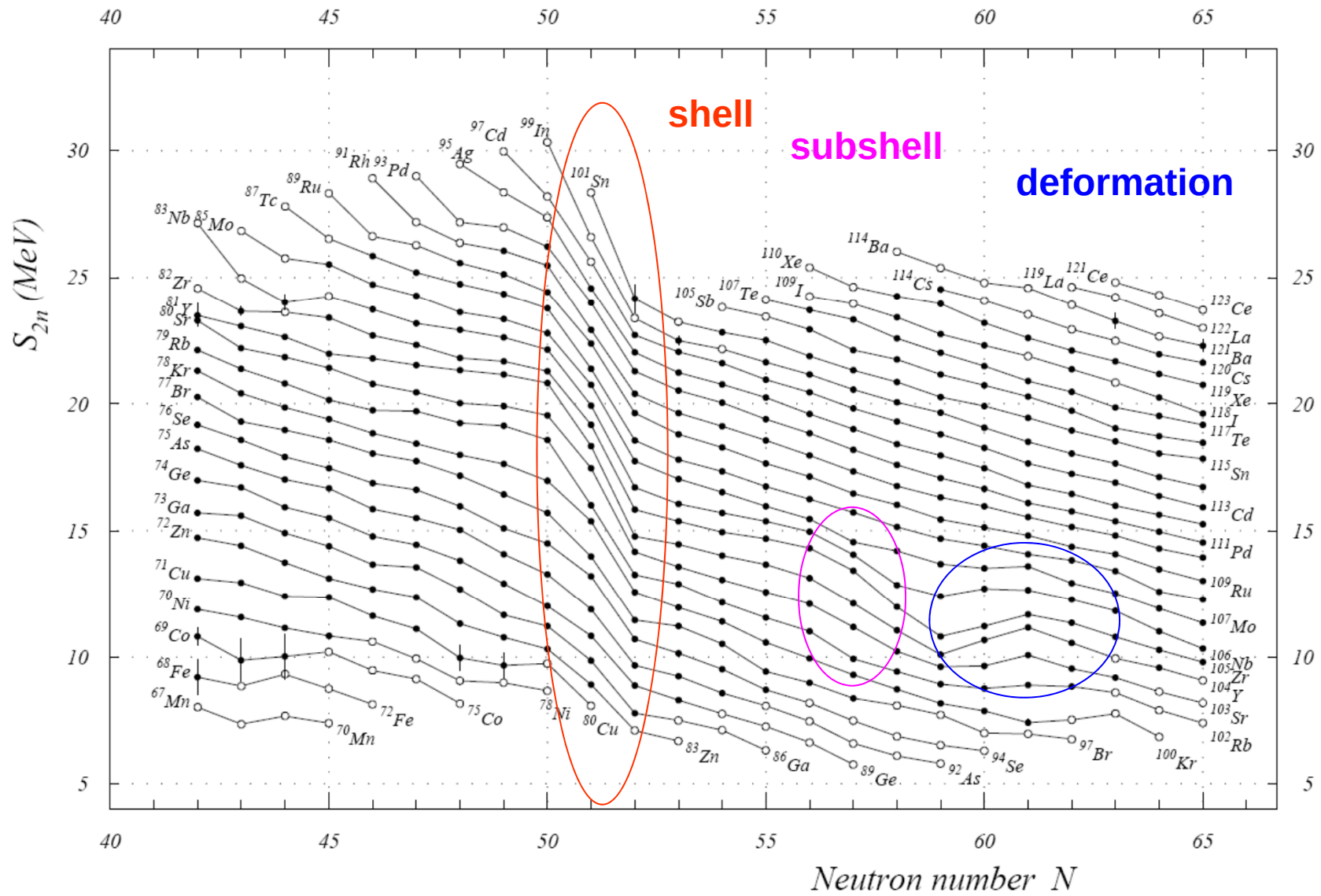
Discoveries

- 1913 : isotopism
- 1919 : age of the Sun
- 1933 : shells
- 1954 : deformed nuclei
- 1974 : magicity may disappear
- 1981 : sub-shells

Discoveries

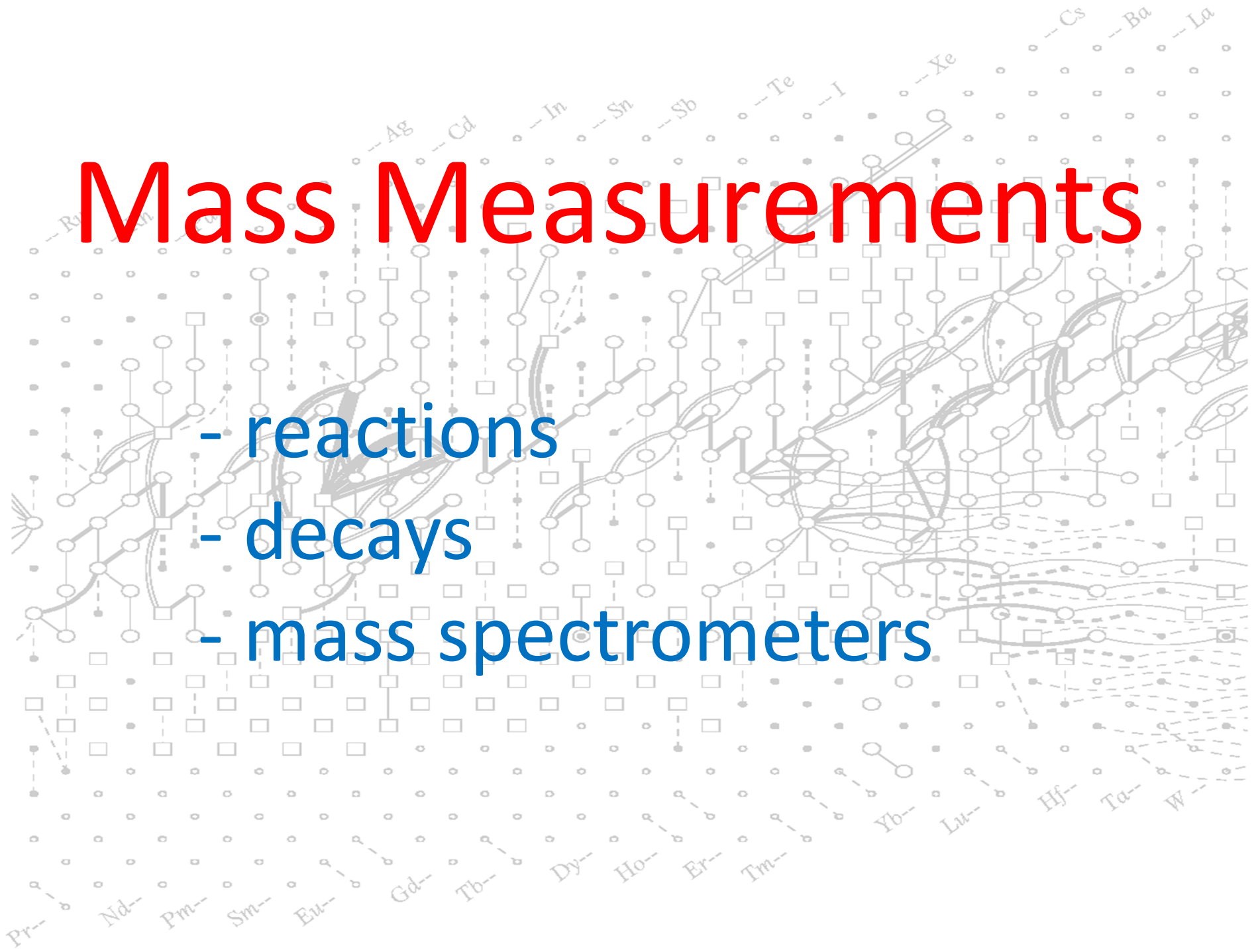
1913	Isotopism ^{20}Ne ^{22}Ne	Thomson
1919	restoring “whole number rule” (e^{-3})	Aston
1919	$H=1.008$ → solving the “age of the Sun crisis”	Aston Eddington
1925	“mass defect” breaking ($8e^{-4}$) full numbers	Aston
1933	closed shells $Z=2$ $Z=8$	Elsasser
1934	$Z=20$ $Z=28$ $Z=50$	Elsasser
1934	$N=126$ with $Z=82$ (alpha decay systs)	Elsasser
1948	“magic numbers” & shell model	Goeppert-Mayer
1954	deformation $N=90$	Hogg & Duckworth
1974	magicity disappearance $N=20$	Klapisch & Thibault
1981	sub-shell closure $N=56$	Audi
1981	deformation $N=60$	Audi

Nuclear structure



Mass Measurements

- reactions
- decays
- mass spectrometers

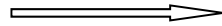


How are atomic masses measured?

Mass measurement:

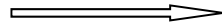
- inertial mass
 - energy
- } **Relative Measurements**

Energy released from
neutron capture of ^{32}S



Mass ratio

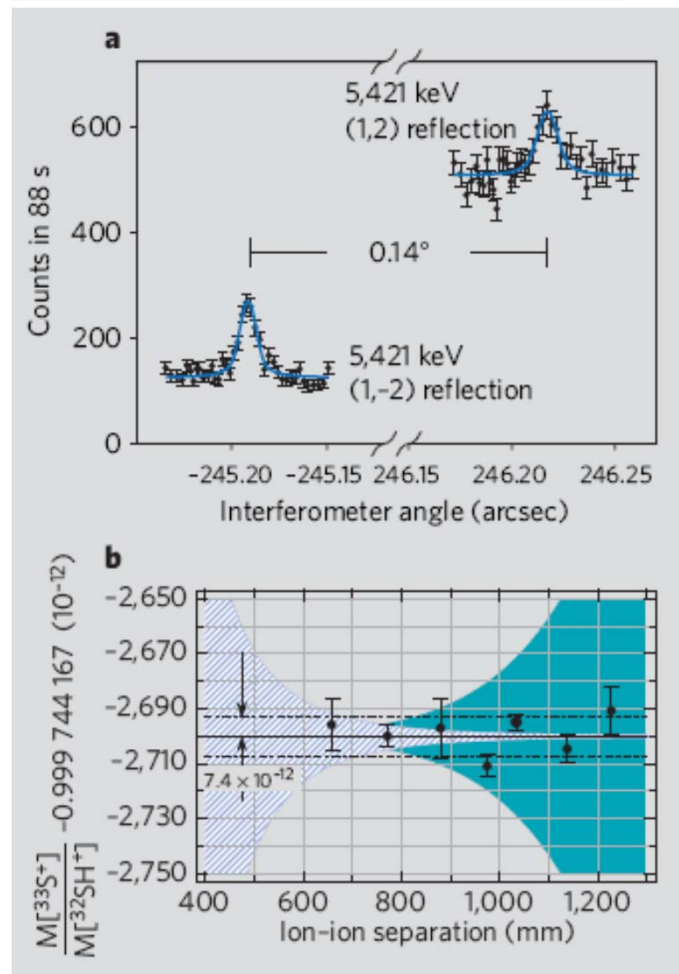
$M[^{33}\text{S}^+]/M[^{32}\text{SH}^+]$



WORLD YEAR OF PHYSICS

A direct test of $E = mc^2$

NATURE|Vol 438|22/29 December 2005



Experimental Data

II

- Reaction Energies eV

$$A(a,b)B \quad Q_r = M_A + M_a - M_b - M_B$$

- close to stability
- (n,γ) and $(p,\gamma) \Rightarrow$ backbone
- self-calibrated $A(a,b)B$ v/s $C(a,b)D$

- Desintegration Energies eV

$$A(\beta^-)B \quad Q_{\beta^-} = M_A - M_B \quad (\text{"Atomic"})$$

$$A(\alpha)B \quad Q_{\alpha} = M_A - M_B - M_{\alpha}$$

$$A(p)B \quad Q_p = M_A - M_B - M_p$$

- far from stability

- Mass Spectrometry u (often called "Direct")

1. Classical Spectrometers
2. Time-of-Flight Spectrometers (M^t ($B\rho$) and velocity)
3. Cyclotron Spectrometers
 - a. Radio-Frequency Spectrometer
 - b. Penning Trap Spectrometer
 - c. Storage Ring Spectrometer

"DIRECT" MASS-MEASUREMENTS (Mass-Spectrometry)

HISTORY of MASS-SPECTROMETRY

For Stable Species : since the origin of Nuclear Physics

Thompson	1907	isotopism in Ne (1912)
Aston	1919	mass - "defect" (1927)
Mattauch	1936	double focussing $R=20.000$
A.O. Nier	1951	spectrography → -metry
Barber	1960	deformation in the rare-earth

For Radioactive Species : 1970's

Pioneers : R. Klapisch and C. Thibault

Li	Na	Rb	Cs	Fr
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TODAY

Measurement of Volts → Measurement of Time (frequencies)

FUTURE

Penning traps - Storage rings

THOMPSON 1907

Champs croisés

$$\begin{aligned} B \rightarrow x &\propto 1/mv^2 \\ E \rightarrow y &\propto 1/mv \\ x &= my^2 \end{aligned}$$

1912 découverte de
l'isotopisme dans
le Ne

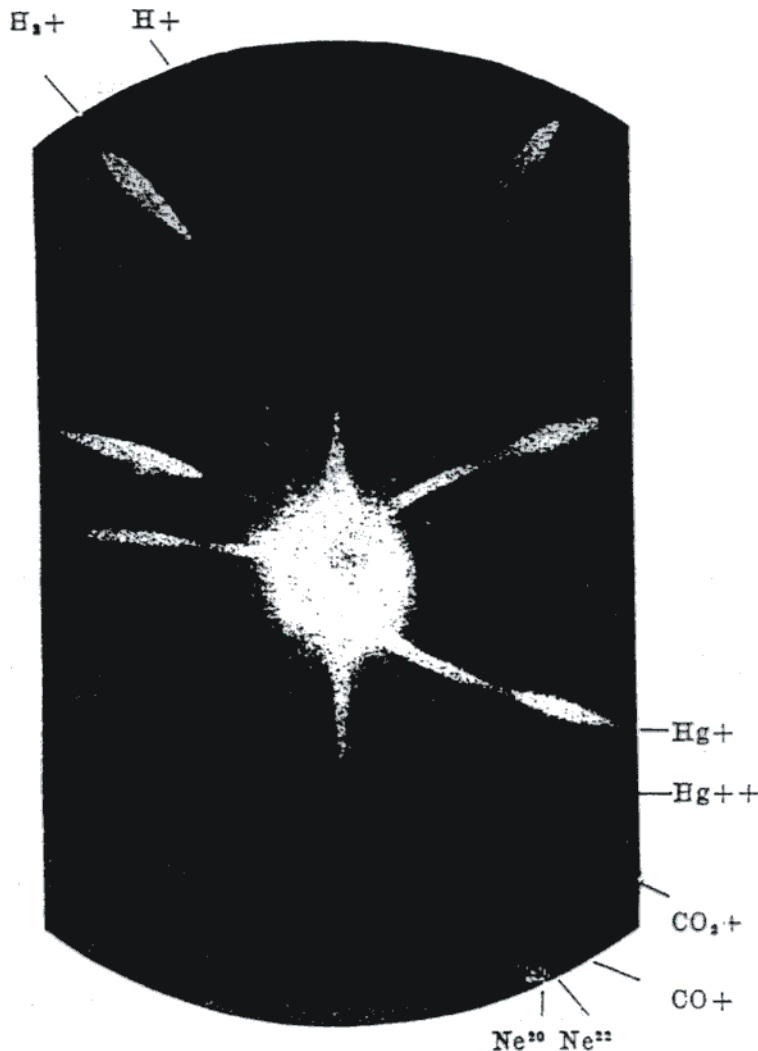


Abb. 82. Kanalstrahlparabeln bei Neonfüllung.

(Aus: F. W. Aston, Isotope. Hirzel, Leipzig.)

"DIRECT" MASS-MEASUREMENTS (Mass-Spectrometry)

HISTORY of MASS-SPECTROMETRY II

For Stable Species : since the origin of Nuclear Physics

For Radioactive Species : 1970's

1971 Klapisch and C. Thibault

PS at CERN : Na and ^{11}Li

first evidence of vanishing shell $N = 20$

1977 Double-Focussing (G.A.) Isolde-II : Rb Cs Fr

subshell-closure at $N = 56$

deformation at $N = 60$

mapping of heavies - pairing - Wigner -

1986 Penning Trap

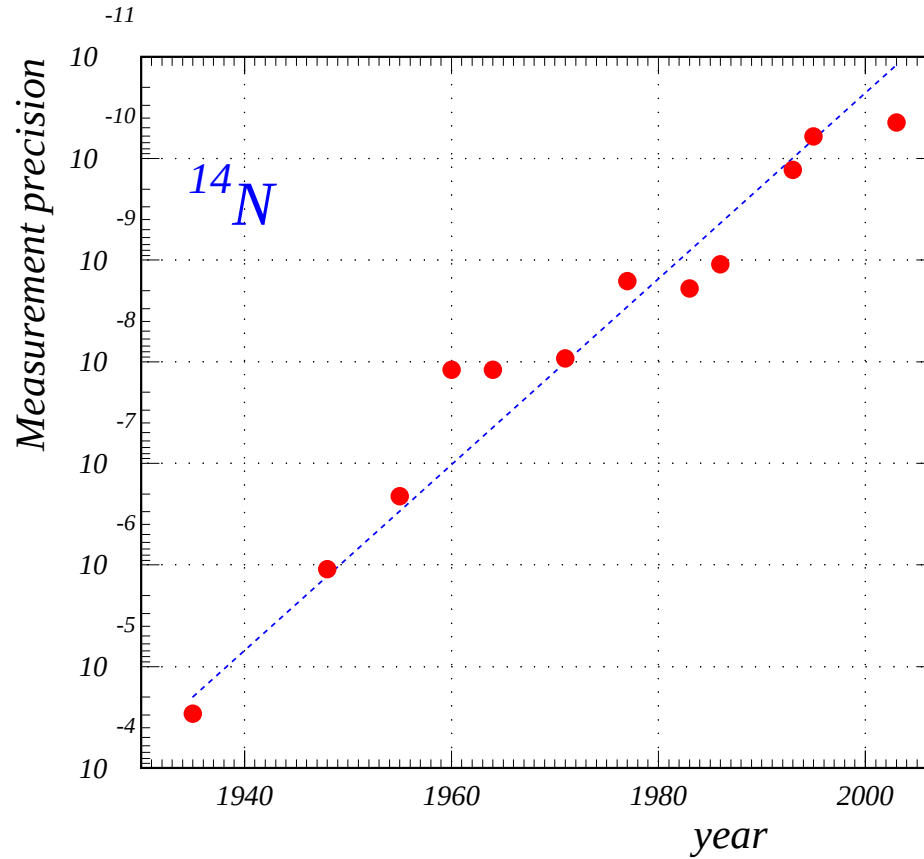
1986 SPEG & TOFI

1994 MISTRAL

1997 ESR-Schottky

2000 ESR-ToF

Precision for ^{14}N

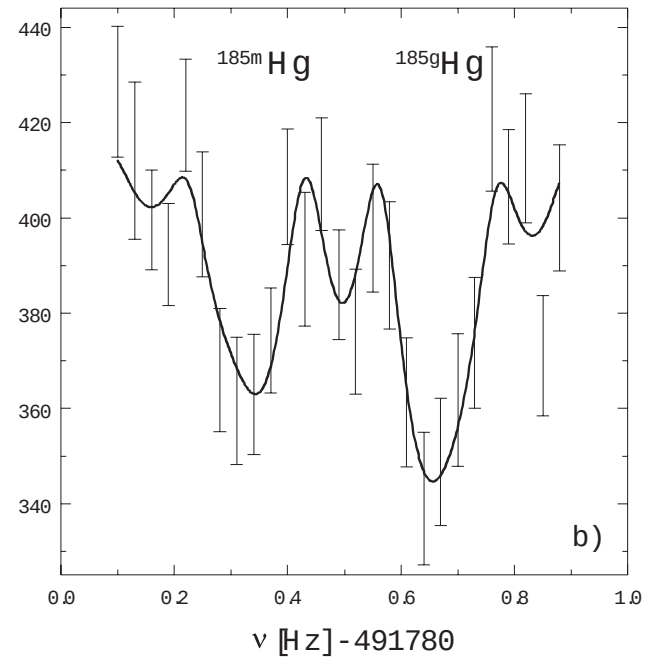
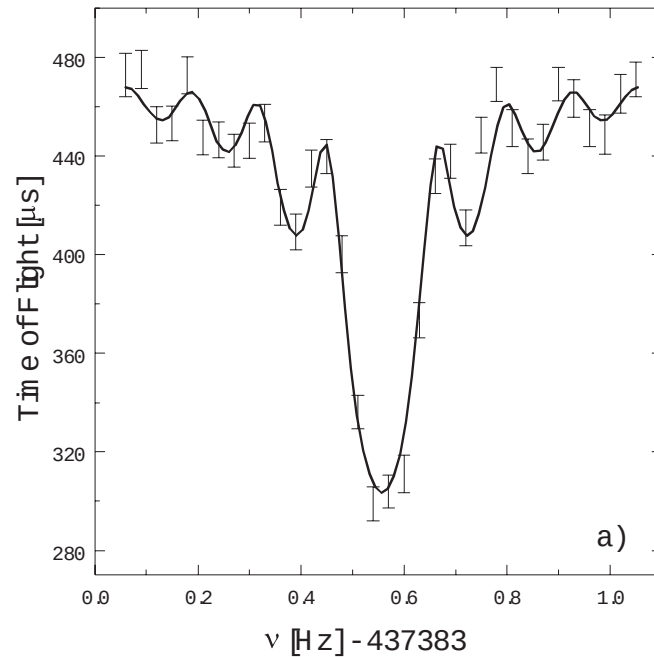


One order of magnitude every 10 years

- 1935: 400 keV
 - 1995: 0.9 eV
 - 2003: 0.5 eV
- 2012 : 0.1 eV

Isomer Separation

- ^{185}Hg - $^{185}\text{Hg}^m$



line width = 50 keV

Isom. Exc. = 104 keV

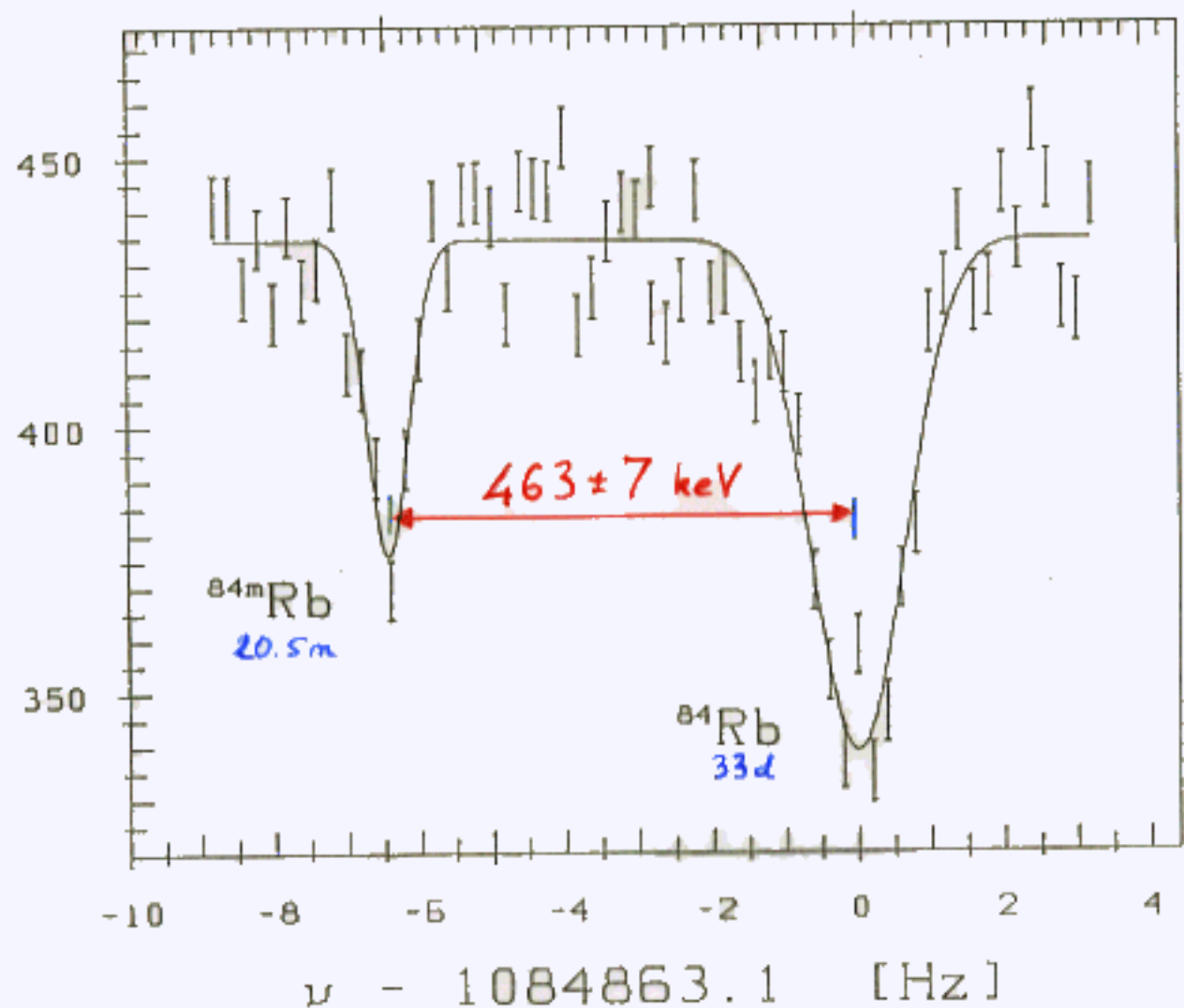
Exc. time = 8 s

Res. Power = 3.7 millions

MASS - 83 914 387.8 [μ u]

600 400 200 0 -200

TIME OF FLIGHT [μ s]



Penning Trap

$463 \pm 7 \text{ keV}$

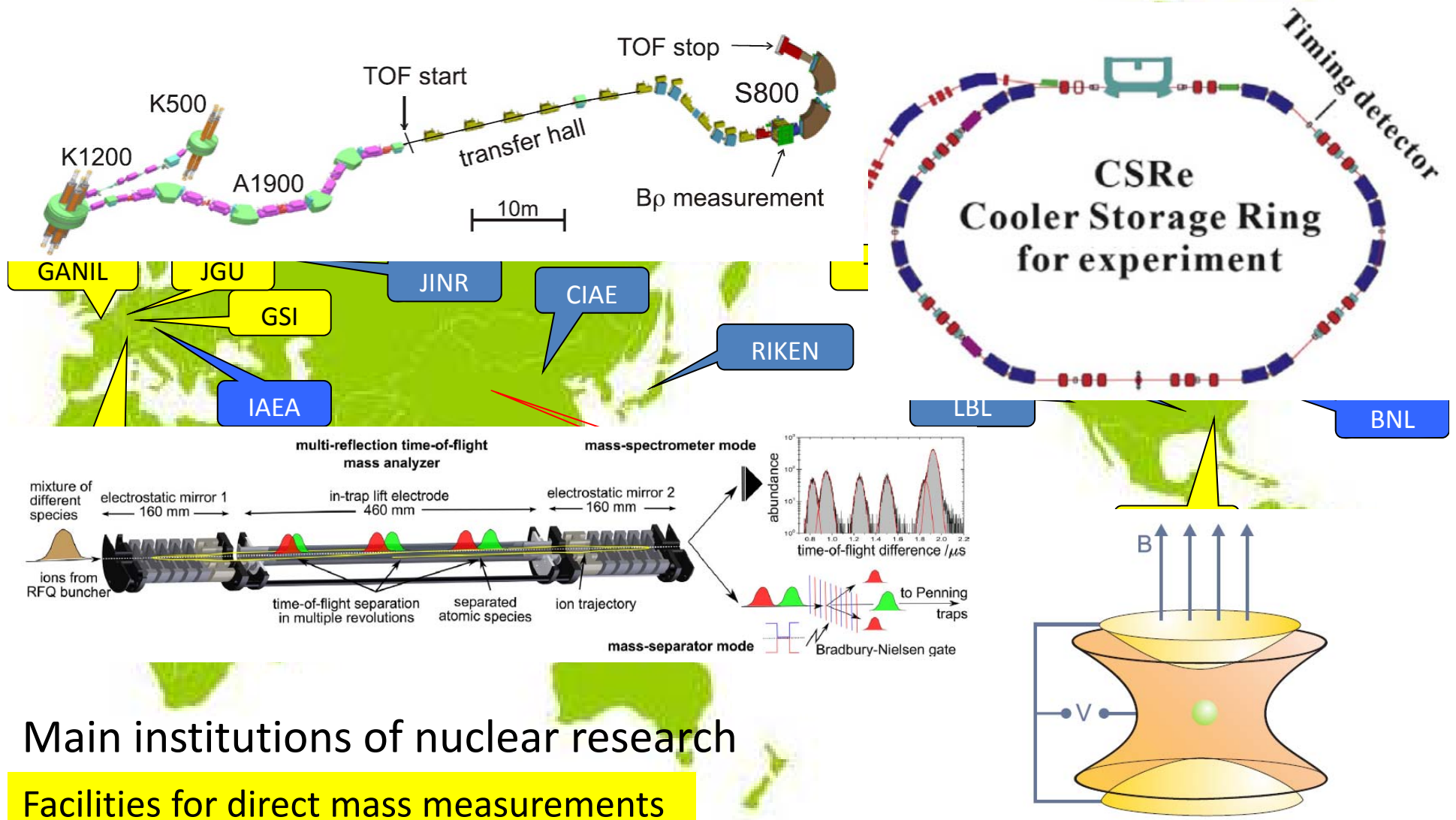
M. König 1991

Litterature

$463.62 \pm .09 \text{ keV}$

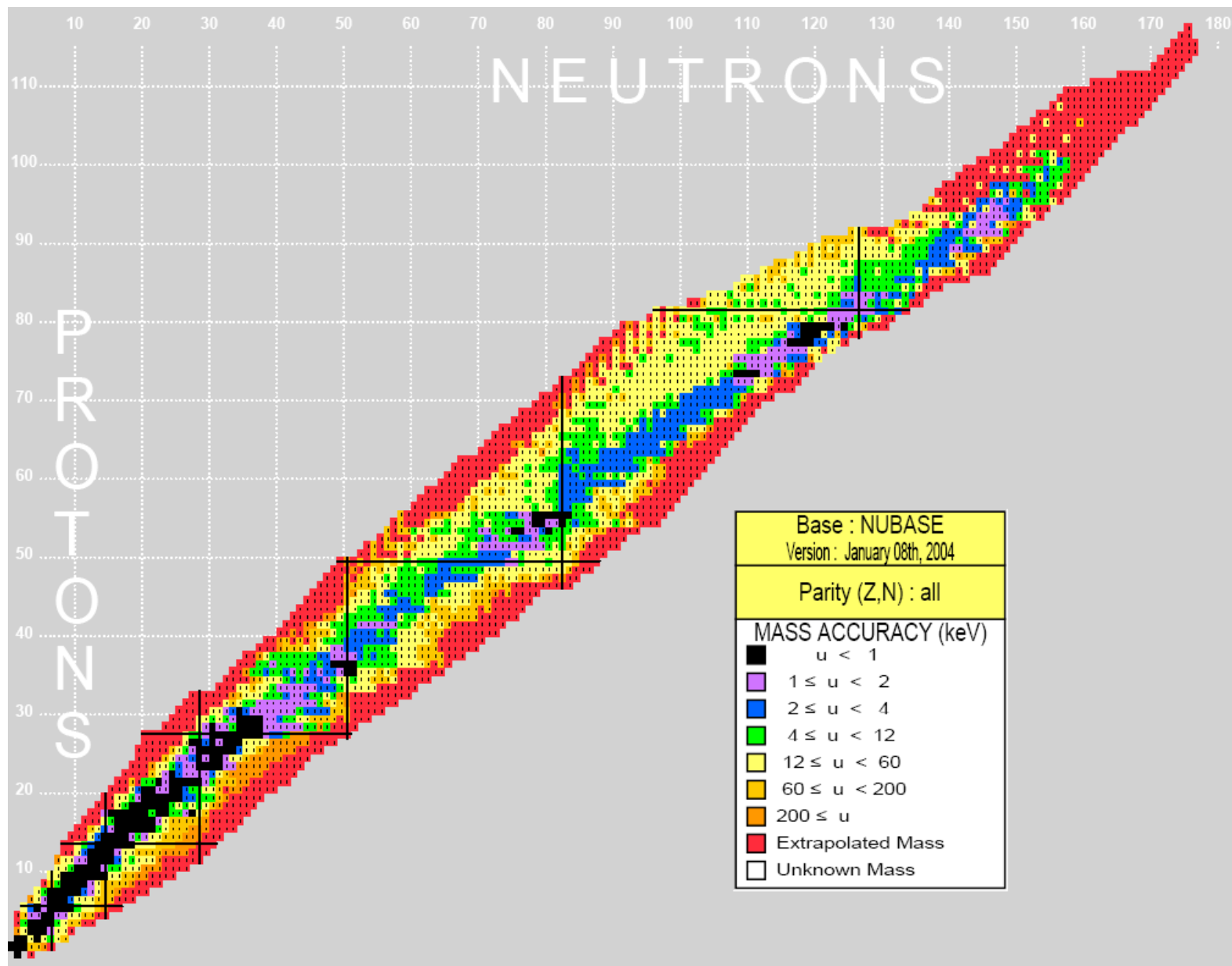
NDS

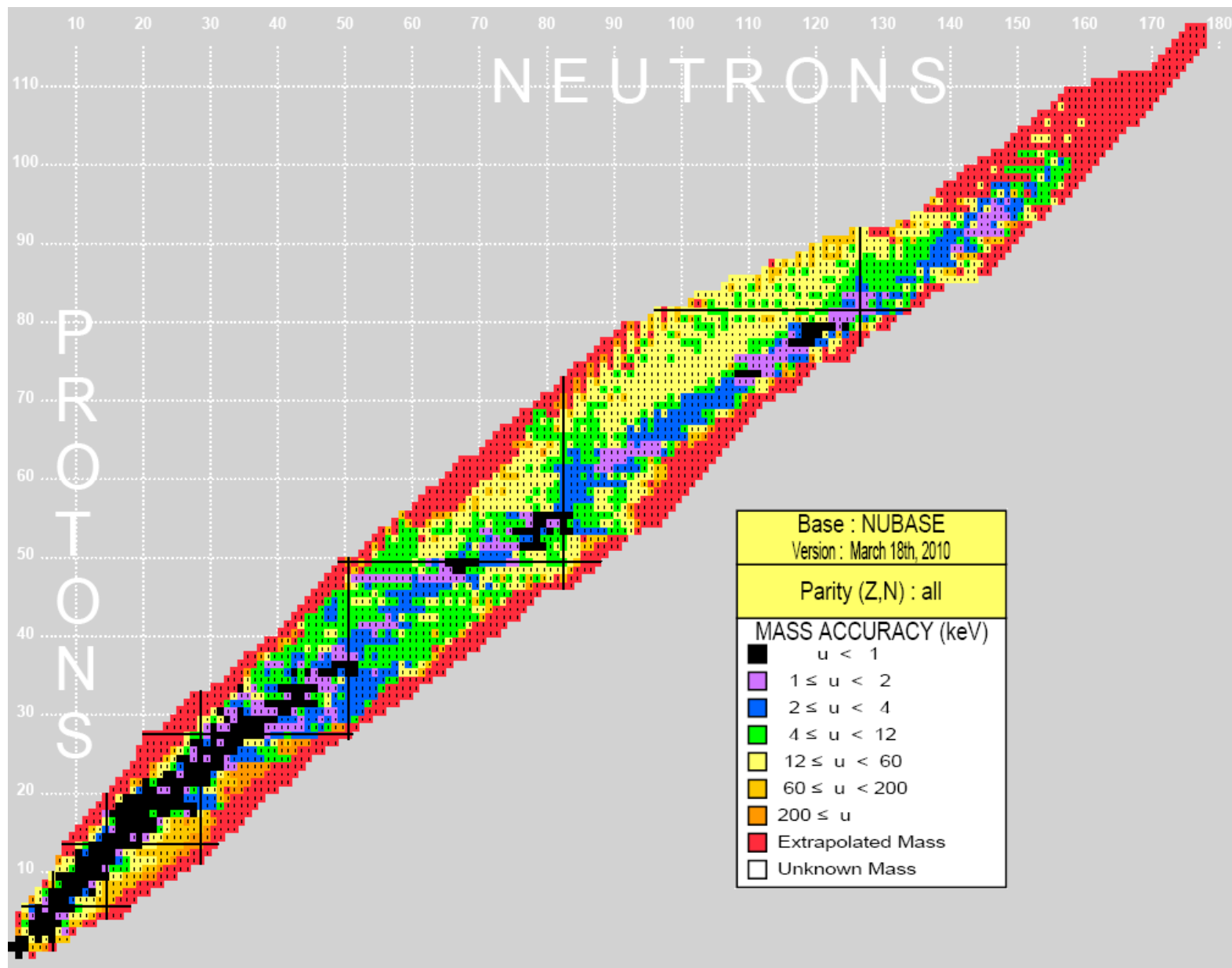
Mass measurements



Main institutions of nuclear research

Facilities for direct mass measurements





Fashions of mass measurements:

Publications in Nature/Science

1. **An Ion Balance for Ultra-High-Precision Atomic Mass Measurements**, S.Rainville, J.K.Thompson, D.E.Pritchard, *Science* 303, 334 (2004)
2. **Cyclotron frequency shifts arising from polarization forces**, J.K.Thompson, S.Rainville, D.E.Pritchard, *Nature(London)* 430, 58 (2004)
3. **A direct test of $E=mc^2$** , S.Rainville, et al., *Nature(London)* 438, 1096 (2005)
4. **Direct mass measurements above uranium bridge the gap to the island of stability**, M.Block et al., *Nature(London)* 463, 785 (2010)
5. **Direct mapping of nuclear shell effects in the heaviest elements**, E. Minaya Ramirez et al., *Science* 337 (6099), 1207-1210 (2012).
6. **Masses of exotic calcium isotopes pin down nuclear forces**, F.Wienholtz et al., *Nature(London)* 498, 346 (2013)

Two frontiers : accuracy, exoticism

Atomic Mass ^3H and ^3He —Using HD^+ as a mass reference

PRL **114**, 013003 (2015)

PHYSICAL REVIEW LETTERS

week ending
9 JANUARY 2015

Atomic Masses of Tritium and Helium-3

E. G. Myers, A. Wagner, H. Kracke, and B. A. Wesson

Department of Physics, Florida State University, Tallahassee, Florida 32306-4350, USA

(Received 11 September 2014; published 7 January 2015)

By measuring the cyclotron frequency ratios of $^3\text{He}^+$ to HD^+ and T^+ to HD^+ , and using HD^+ as a mass reference, we obtain new atomic masses for ^3He and T. Our results are $M[^3\text{He}] = 3.016\,029\,322\,43(19)$ u and $M[\text{T}] = 3.016\,049\,281\,78(19)$ u, where the uncertainty includes an uncertainty of 0.12 nu in the mass reference. Allowing for cancellation of common systematic errors, we find the Q value for tritium β decay to be $(M[\text{T}] - M[^3\text{He}])c^2 = 18\,592.01(7)$ eV. This allows an improved test of systematics in measurements of tritium β decay that set limits on neutrino mass.

Unc.= 0.2 eV

Detailed calculation for mass HD

Atomic masses and the mass difference between tritium and helium-3.—Using the 2010 CODATA values for the masses of the electron, proton, and deuteron [9] combined with the ground-state energy of HD^+ relative to its separated constituents [25], we predict the atomic mass of the HD^+ ion to be 3.021 378 241 97(12) u, where the uncertainty is due to the uncertainty in the masses of the

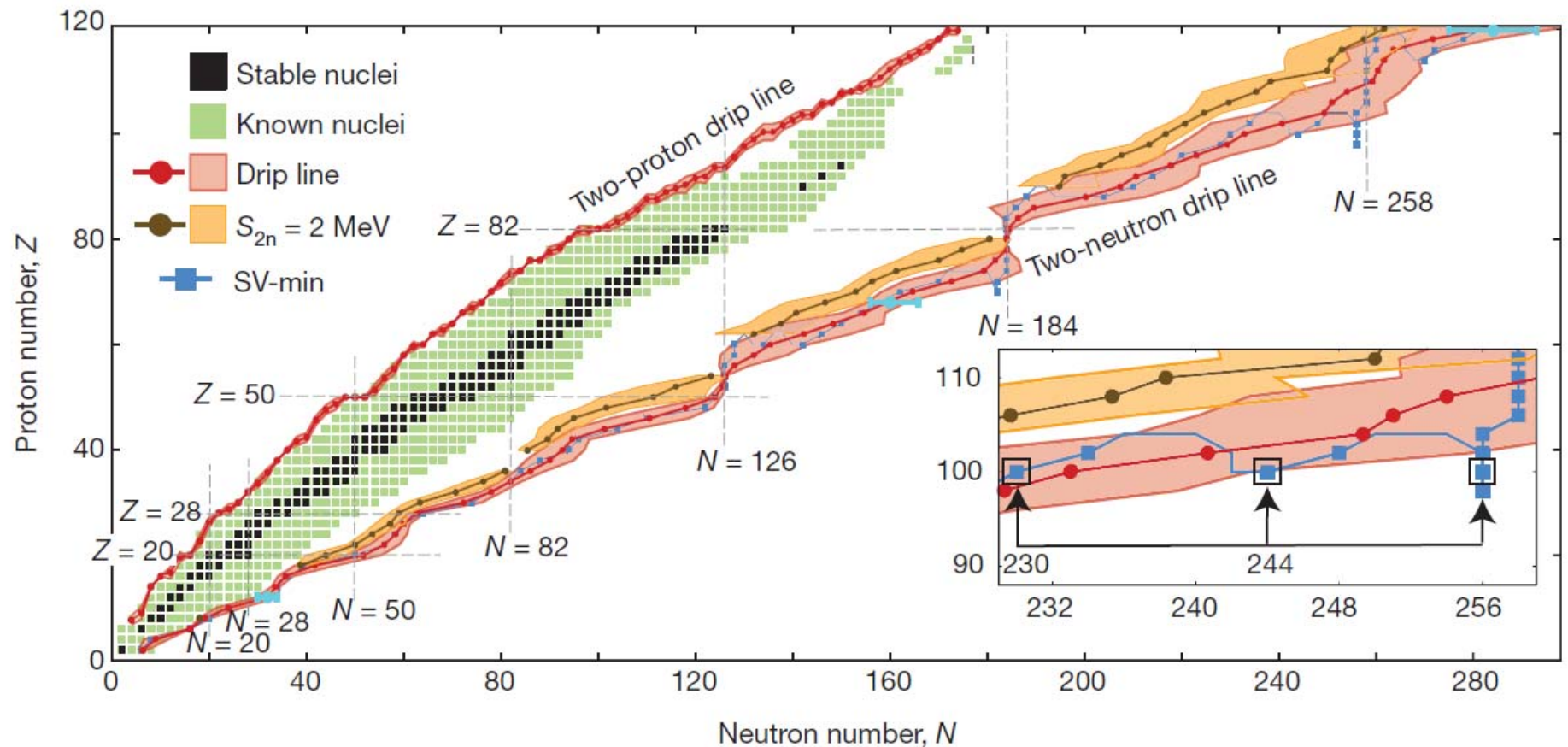
Ame2012	1H	1 007 825 032.23	(09)	(0.093nu)
	2H	2 014 101 778.12	(12)	(0.122nu)
H+D	=	3 021 926 810.35	(14)	(0.136nu)
BEmol	-	4.85		
HD molec.=		3 021 926 805.50		
me	-	548 579.91		
BEE(+)	+	16.58		
HD+	=	3 021 378 242.17	(14)	
compared to				
2015Myers		3 021 378 241.97	(12)	
The difference is		0.20	(14)	1.4 sigma

Exotic nuclei

The limits of the nuclear landscape

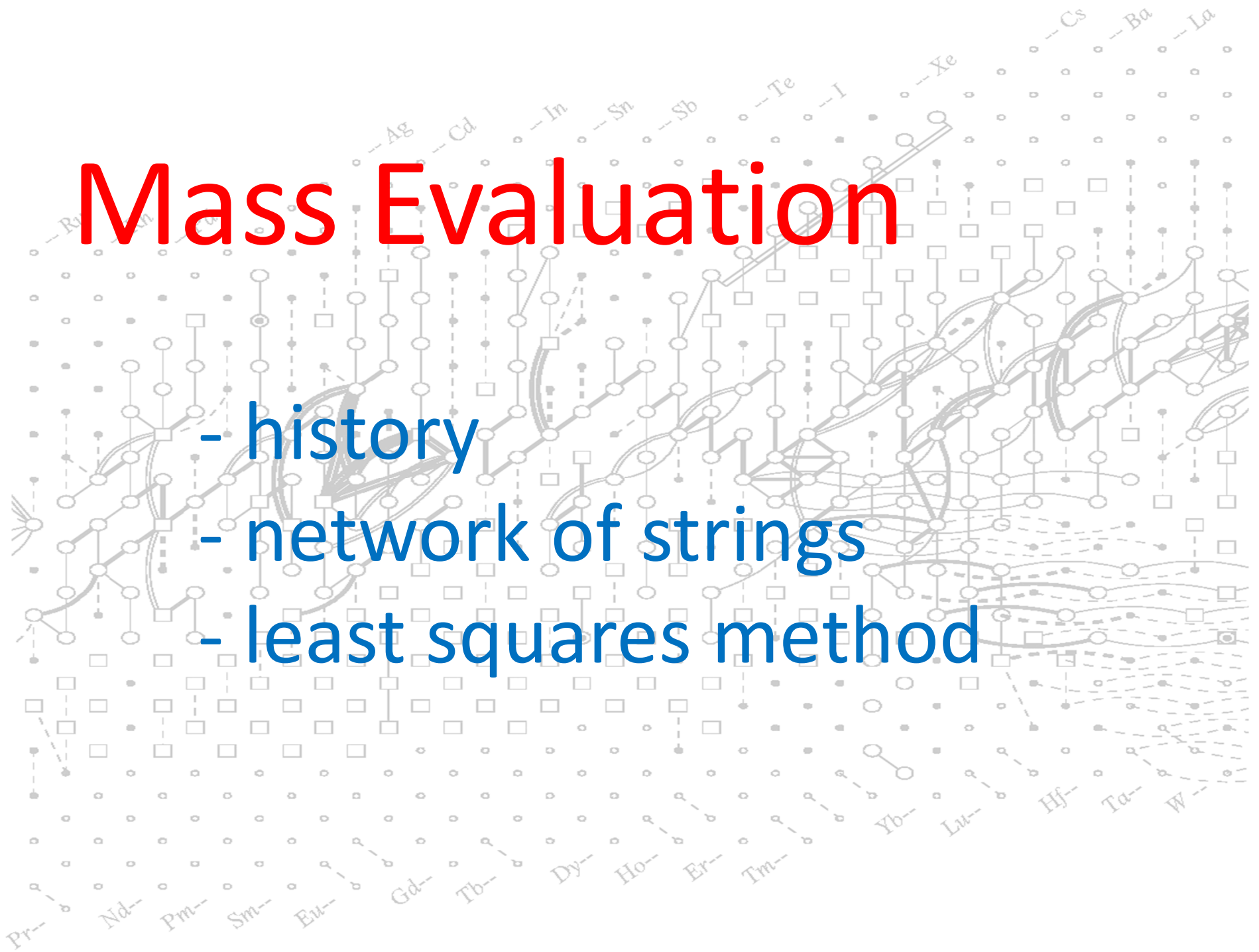
doi:10.1038/nature11188

Jochen Erler^{1,2}, Noah Birge¹, Markus Kortelainen^{1,2,3}, Witold Nazarewicz^{1,2,4}, Erik Olsen^{1,2}, Alexander M. Perhac¹ & Mario Stoitsov^{1,2,†}



Mass Evaluation

- history
- network of strings
- least squares method



60 years of mass evaluations

A history of atomic masses can be found in:

Georges Audi

“The history of nuclidic masses and of their evaluation”

International Journal of Mass Spectrometry 251 (2006) 85–94

An early (perhaps the first) attempt for a mass evaluation is

M.S. Livingston, H.A. Bethe, “Nuclear Physics, C. Nuclear dynamics, experimental”,
Rev. Mod. Phys. 9 (1937) 245, XVIII. Nuclear masses; p. 366

The authors combined data from mass spectrometry and nuclear reaction and decay data up to ^{40}Ar .

In the early 1950's it was found that the many relations (direct and indirect) overdetermined the mass value of many nuclides.

Aaldert H. Wapstra established a procedure using a least-squares method to solve the problem of overdetermination.

The first table of atomic masses using this method is dated 1955.

60 years of mass evaluation

**Ame1955, Ame1961, Ame1964,
Ame1971, Ame1977, Ame1983,
Ame1993, Ame2003, Ame2012
and now : **Ame2016****

will appear in CPC in December 2016

(but with no reprints)

to keep closer to experimental life and new
results

60 years of mass evaluation

History of Wapstra's type mass tables

A.H. Wapstra, [Physica 21 \(1955\) 367 + 385](#); J.R. Huizenga, [Physica 21 \(1955\) 410](#)

F. Everling, L.A. König, J.H.E. Mattauch, A.H. Wapstra, [Nucl. Phys. 18 \(1960\) 529](#)

L.A. König, J.H.E. Mattauch, A.H. Wapstra, [Nucl. Phys. 31 \(1962\) 18](#)

J.H.E. Mattauch, W. Thiele, A.H. Wapstra, [Nucl. Phys. A67 \(1965\) 1 + 32 + 73](#)

A.H. Wapstra, K. Bos, [At. Data Nucl. Data Tables 19 \(1977\) 175](#)

A.H. Wapstra, G. Audi, R. Hoekstra, [Nucl. Phys. A432 \(1985\) 185](#)

G. Audi, A.H. Wapstra, [Nucl. Phys. A 565 \(1993\) 66](#)

C. Borcea, G. Audi, A.H. Wapstra, P. Favaron, [Nucl. Phys. A 565 \(1993\) 158](#)

G. Audi, A.H. Wapstra, M. Dedieu, [Nucl. Phys. A 565 \(1993\) 193](#)

G. Audi & A.H. Wapstra, [Nucl. Phys. A 595 \(1995\) 409](#) ; an update

A.H. Wapstra, G. Audi, C. Thibault, [Nucl. Phys. A 729 \(2003\) 129](#)

G. Audi, A.H. Wapstra, C. Thibault, [Nucl. Phys. A 729 \(2003\) 337](#)

G. Audi, M. Wang, A. H. Wapstra, F. G. Kondev, M. MacCormick, X. Xu, B. Pfeiffer,
[Chinese Physics C 36 \(2012\) 1287](#)

M. Wang, G. Audi, A. H. Wapstra, F. G. Kondev, M. MacCormick, X. Xu, B. Pfeiffer,
[Chinese Physics C 36 \(2012\) 1603](#)

AME2012

December 2012 issue of Chinese Physics C (IOP Science)

Volume 36 Number 12 December 2012



1157 The NUBASE2012 evaluation of nuclear properties

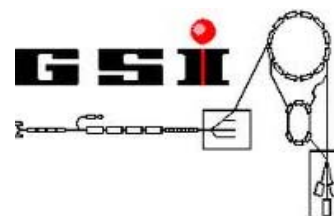
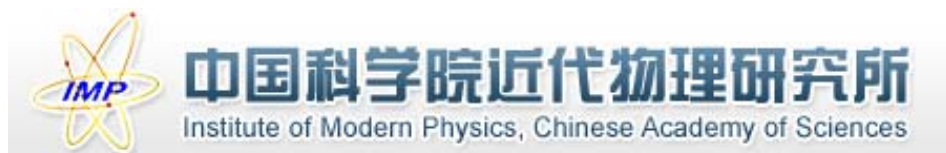
G. Audi, F.G. Kondev, M. Wang, B. Pfeiffer, X. Sun, J. Blachot, M. MacCormick

1287 The AME2012 atomic mass evaluation (I). Evaluation of input data, adjustment procedures

G. Audi, M. Wang, A.H. Wapstra, F.G. Kondev, M. MacCormick, X. Xu, B. Pfeiffer

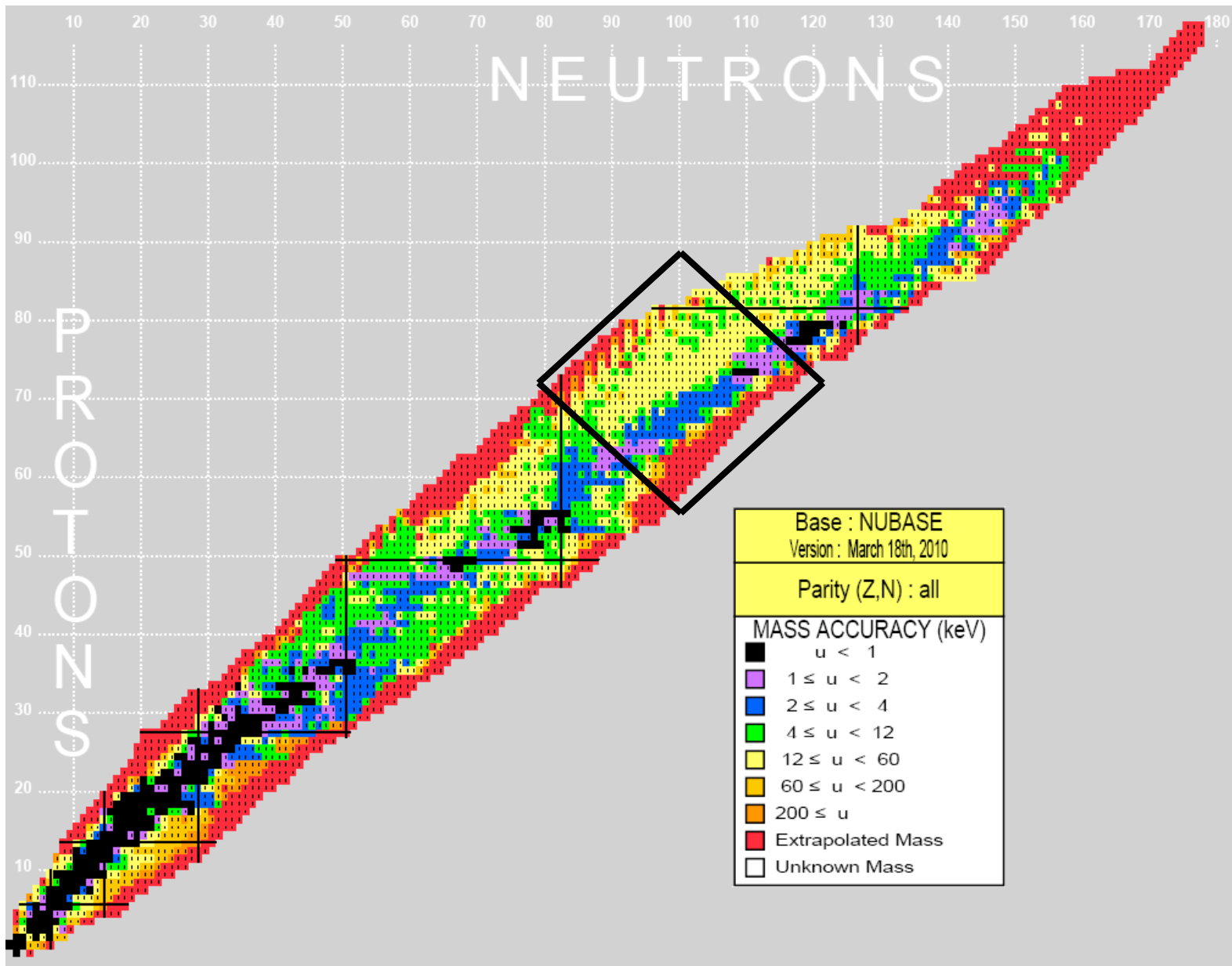
1603 The AME2012 atomic mass evaluation (II). Tables, graphs and references

M. Wang, G. Audi, A.H. Wapstra, F.G. Kondev, M. MacCormick, X. Xu, B. Pfeiffer



Evaluation of Nuclear Data

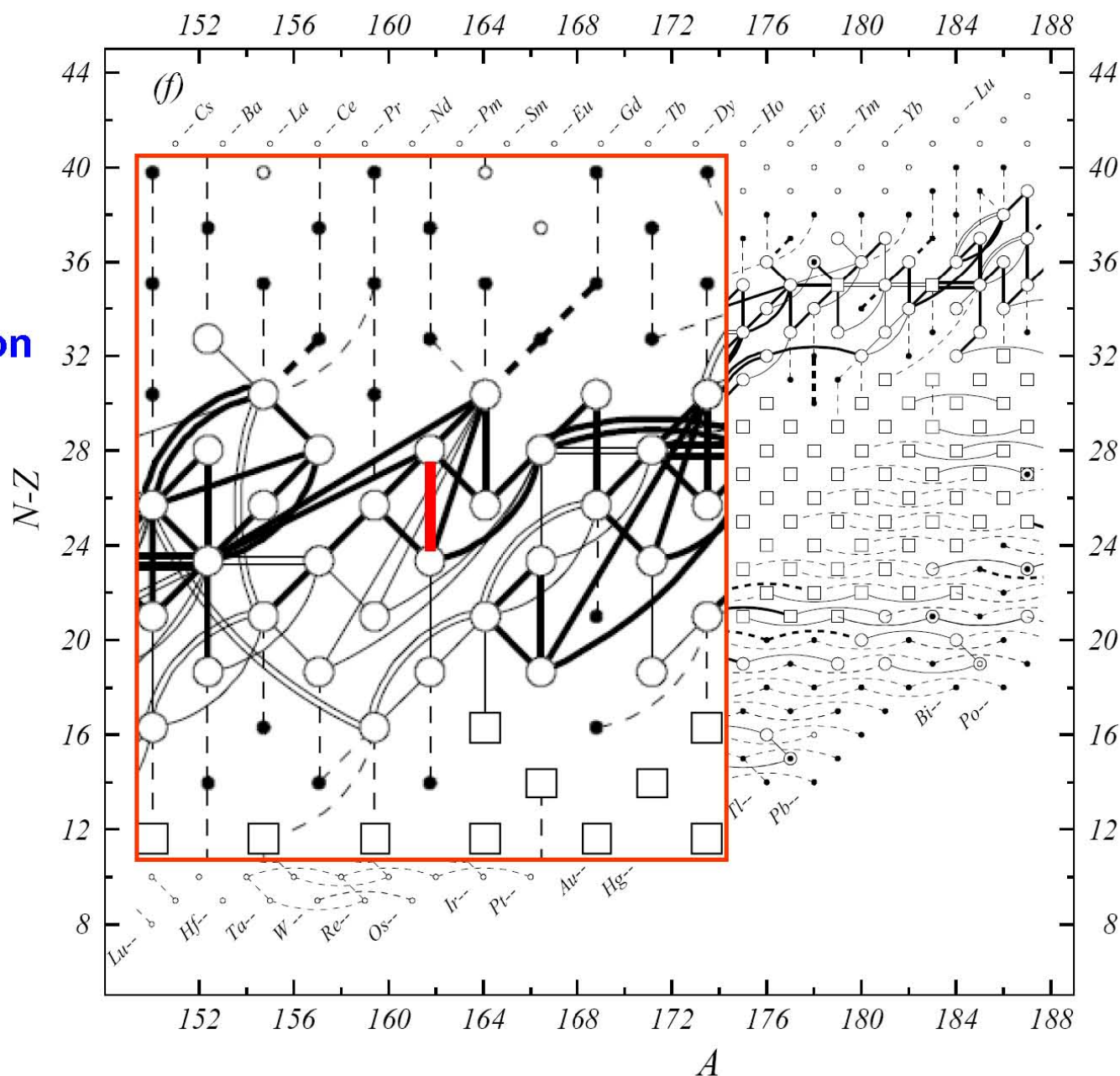
- Theoretical evaluation (= theoretical predictions)
 - predict values for large sets of nuclei
 - make effective calculations for : r-process - reactors - ...
 - uncertainties : just starting security $\Leftrightarrow$ feasibility
- Evaluation of experimental data
 - basic blocks : results from experiments
 - if available : preferred to theoretical predictions
 - allows also to test theoretical “evaluations”



Atomic Mass Evaluation

Evaluation $\neq$ Compilation

Atomic masses are extracted from the complex network of string tensions.



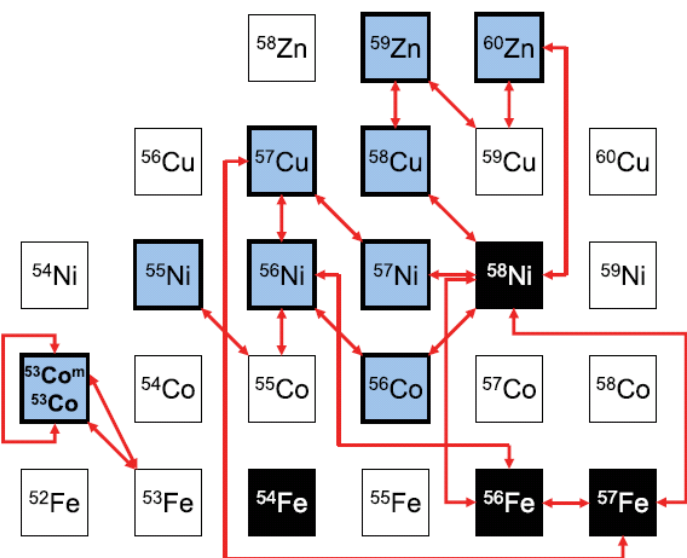
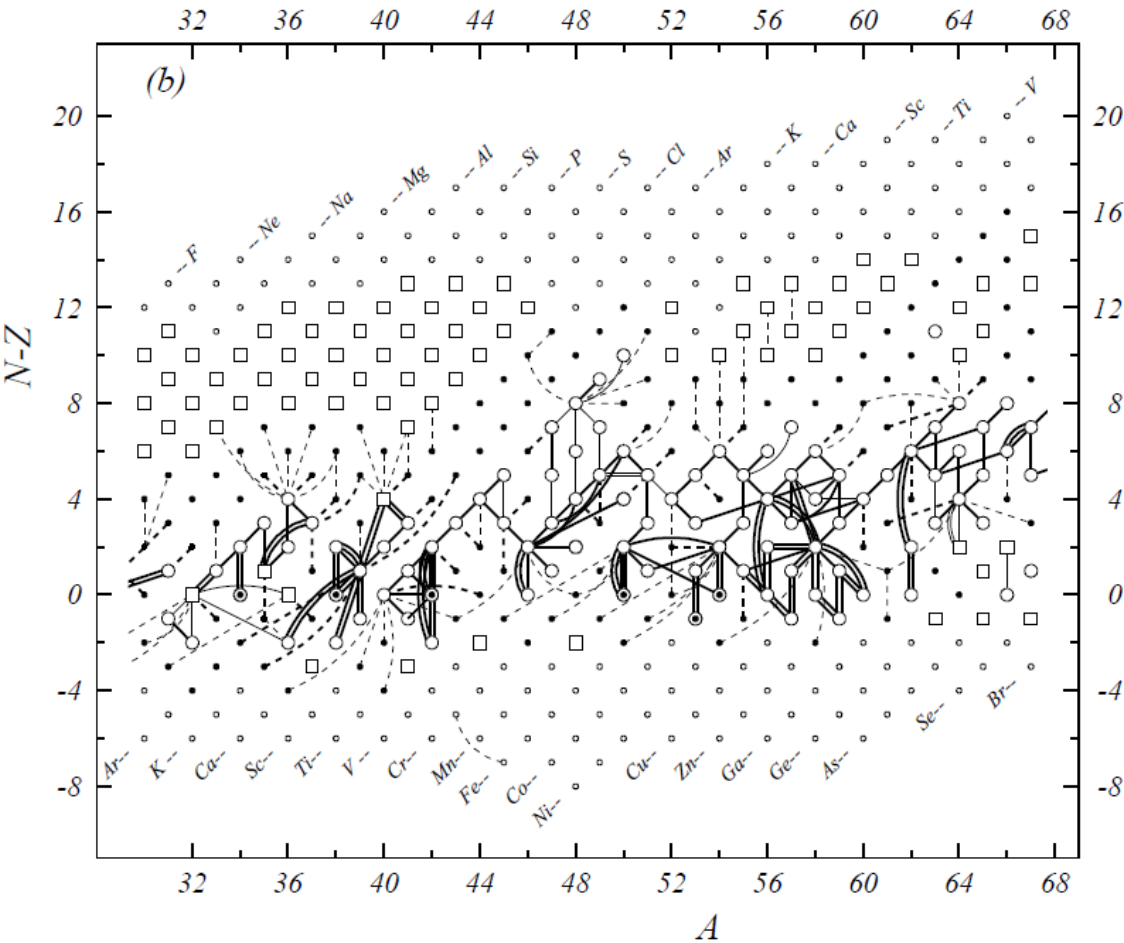


FIG. 2. (Color online) The highlighted nuclides were measured in this work. The red arrows show the measured frequency ratio pairs.

[A.Kankainen](#) et al.,
 Phys.Rev. C 82, 034311 (2010)



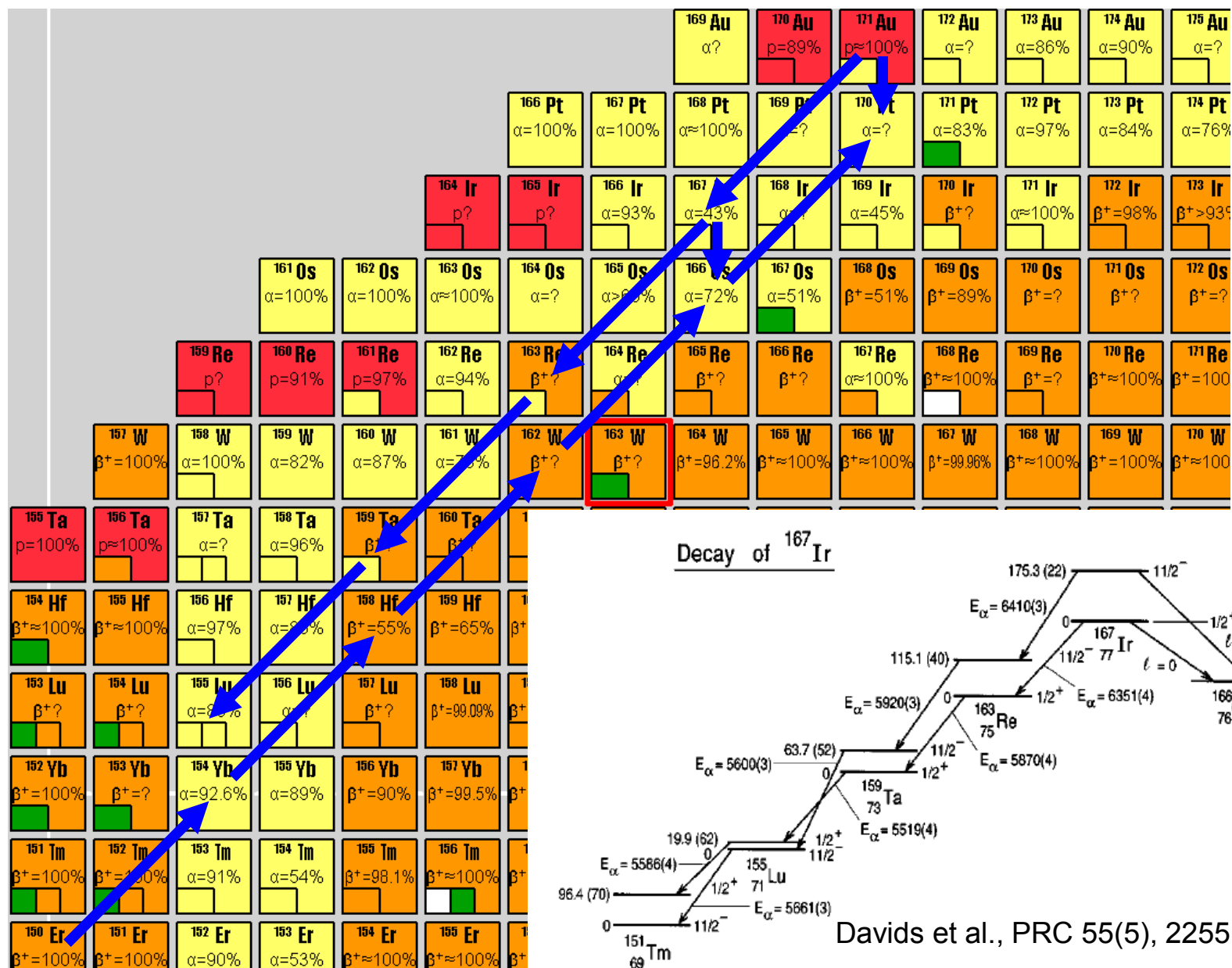


FIG. 14. Decay scheme of correlated alphas from ^{167}Ir .

Experimental Data

- Energy Relation

expressed in eV or keV

keV*: *standard* volt

adopt a value for $2e/h$ in Josephson

keV: *international* volt

from evaluation of fundamental constants

- Inertial mass in EM field

expressed in u or μu , the

“unified mass unit”

$1u = \mathcal{M}(^{12}\text{C})/12$ since 1960

Conversion factor:

$$1u = 931\,494.009\,0 \pm 0.007\,1 \text{ keV}^*$$

$$1u = 931\,494.013 \pm 0.037 \text{ keV}$$

Treatment of Data -

LSM - 1

Q data $q_i \pm dq_i$

M unknown quantities m_μ with $Q > M$

Q equations to M parameters overdetermined

$$\sum_{\mu=1}^M k_i^\mu m_\mu = q_i \pm dq_i \Rightarrow \boxed{\mathbf{K}|m\rangle = |q\rangle}$$

and the diagonal weight matrix $\mathbf{W} : w_i^i = 1/(dq_i dq_i)$

Very simple construction

$${}^t\mathbf{K}\mathbf{W}\mathbf{K}|m\rangle = {}^t\mathbf{K}\mathbf{W}|q\rangle$$

$$\mathbf{A}|m\rangle = {}^t\mathbf{K}\mathbf{W}|q\rangle$$

$\mathbf{A}$ normal matrix square, positive, symmetric and regular

$\Rightarrow$ invertible : $\mathbf{A}^{-1}$

$$|\overline{m}\rangle = \mathbf{A}^{-1} {}^t\mathbf{K}\mathbf{W}|q\rangle \Rightarrow \boxed{|\overline{m}\rangle = \mathbf{R}|q\rangle}$$

“Flow-of-information” matrix : $\Rightarrow$

$$\boxed{\mathbf{F} = {}^t\mathbf{R} \otimes \mathbf{K}}$$

NIM 249 (1986) 443

Treatment of Data -

LSM - 1a

$$\text{adj. value of exp. data} \Rightarrow |\bar{q}\rangle = \mathbf{KR}|q\rangle$$

Consistency of data

$$v_i = (\bar{q}_i - q_i)/dq_i \Rightarrow \chi^2 = \sum_{i=1}^Q v_i^2$$

$$\text{expected} \quad \chi_{\text{expect}} = Q - M \pm \sqrt{2(Q - M)}$$

normalized χ_n = consistency factor = Birge ratio

$$\chi_n = \sqrt{\chi^2/(Q - M)} \quad \chi_{n-\text{expected}} = 1 \pm 1/\sqrt{2(Q - M)}$$

Partial consistency factor, χ_n^p , for a group of p data:

$$\chi_n^p = \sqrt{\frac{Q}{Q - M} \frac{1}{p} \sum_{i=1}^p v_i^2}.$$

Present status

Statistics

Input data

13809 input equations

5275 mass spectrometry

8534 reactions

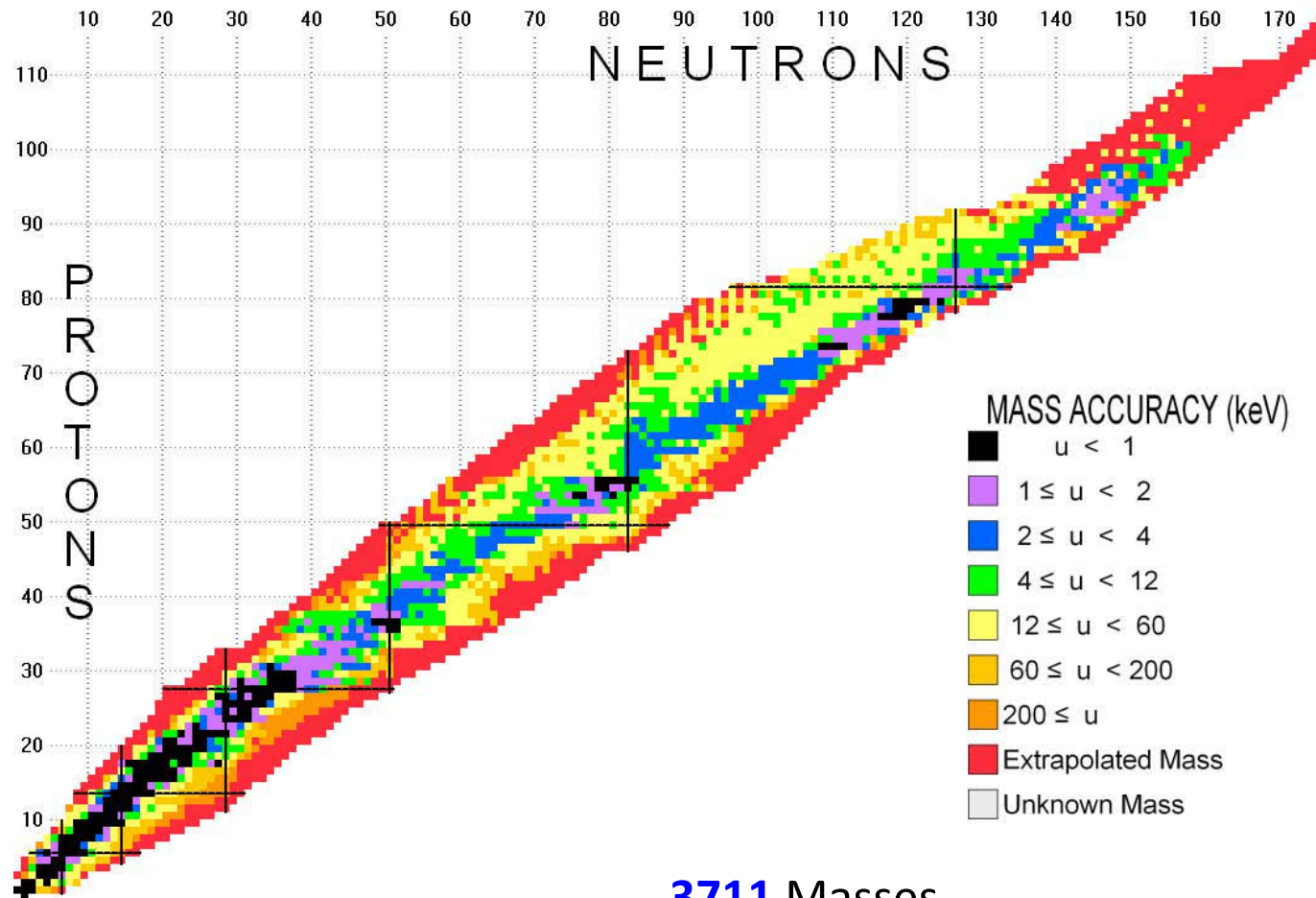
3711 Masses

2416 known ground state

232 known isomers

1063 estimated

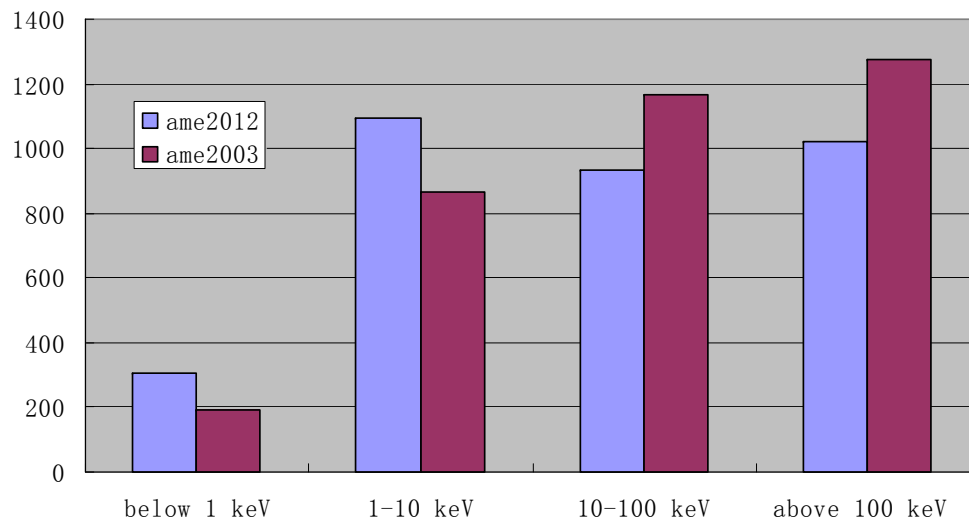
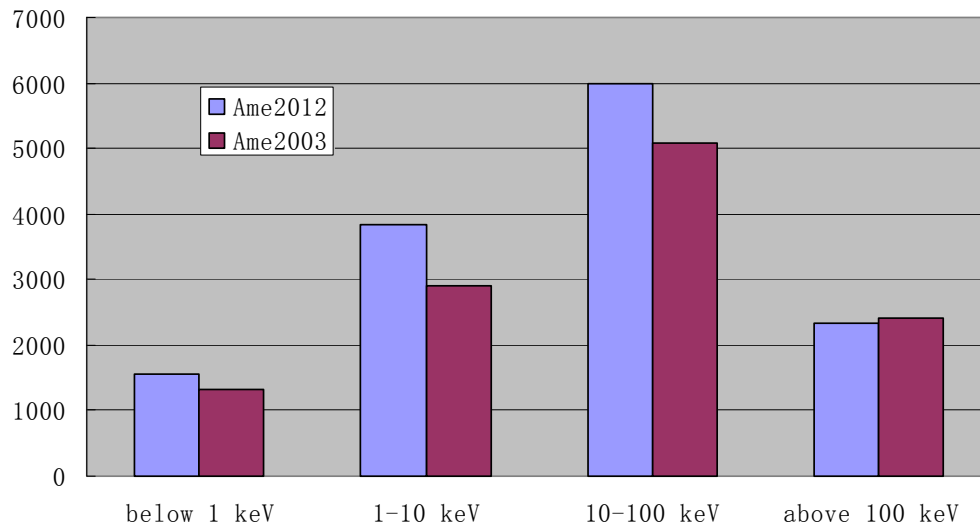
Accuracy of mass values



13809 input equations in **AME12**
5275 mass spectrometry
8534 reactions & decays

3711 Masses
2416 known ground state
232 known isomers
1063 extrapolated

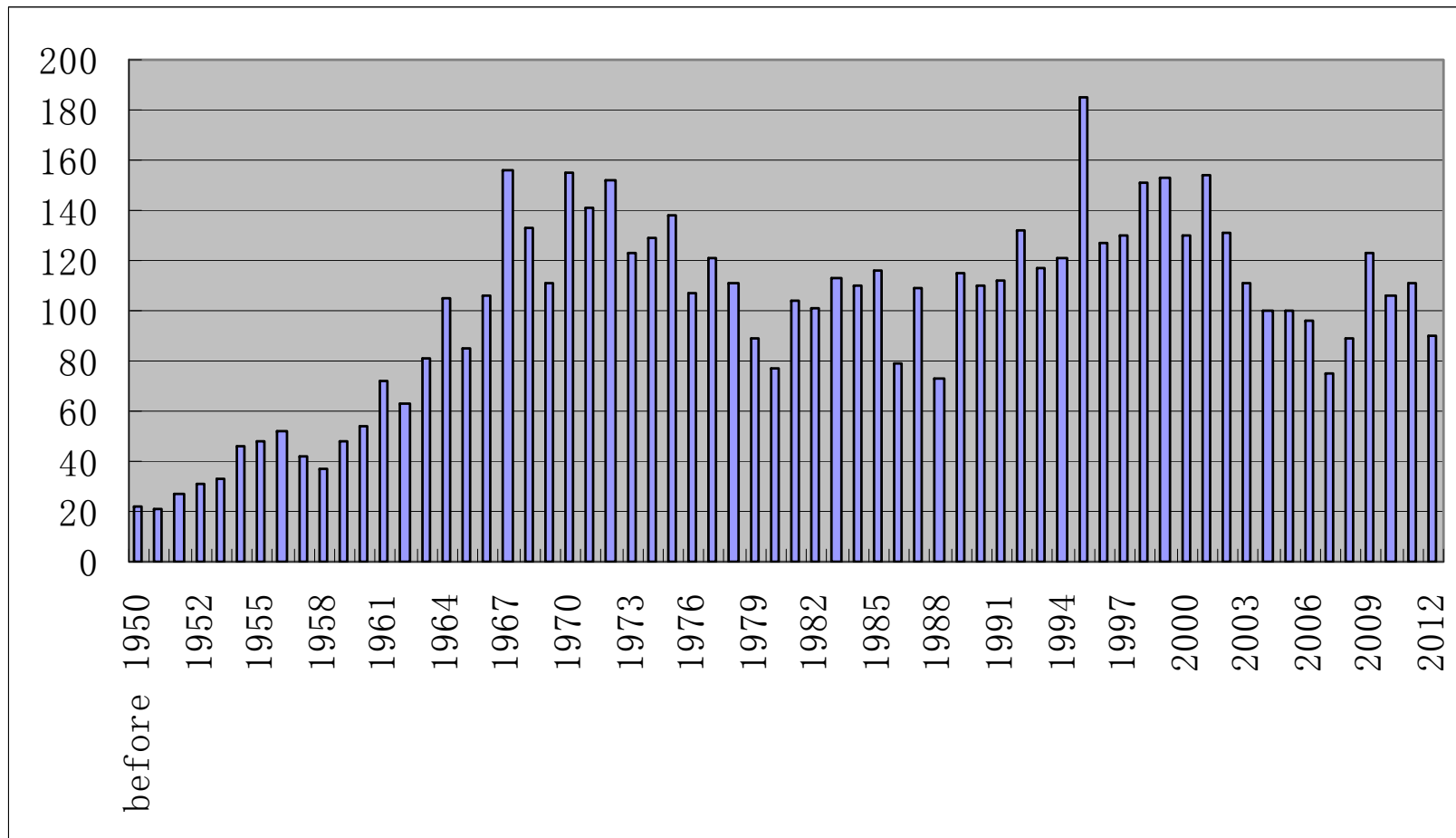
Precisions in Ame2003 v/s Ame2012



Input data

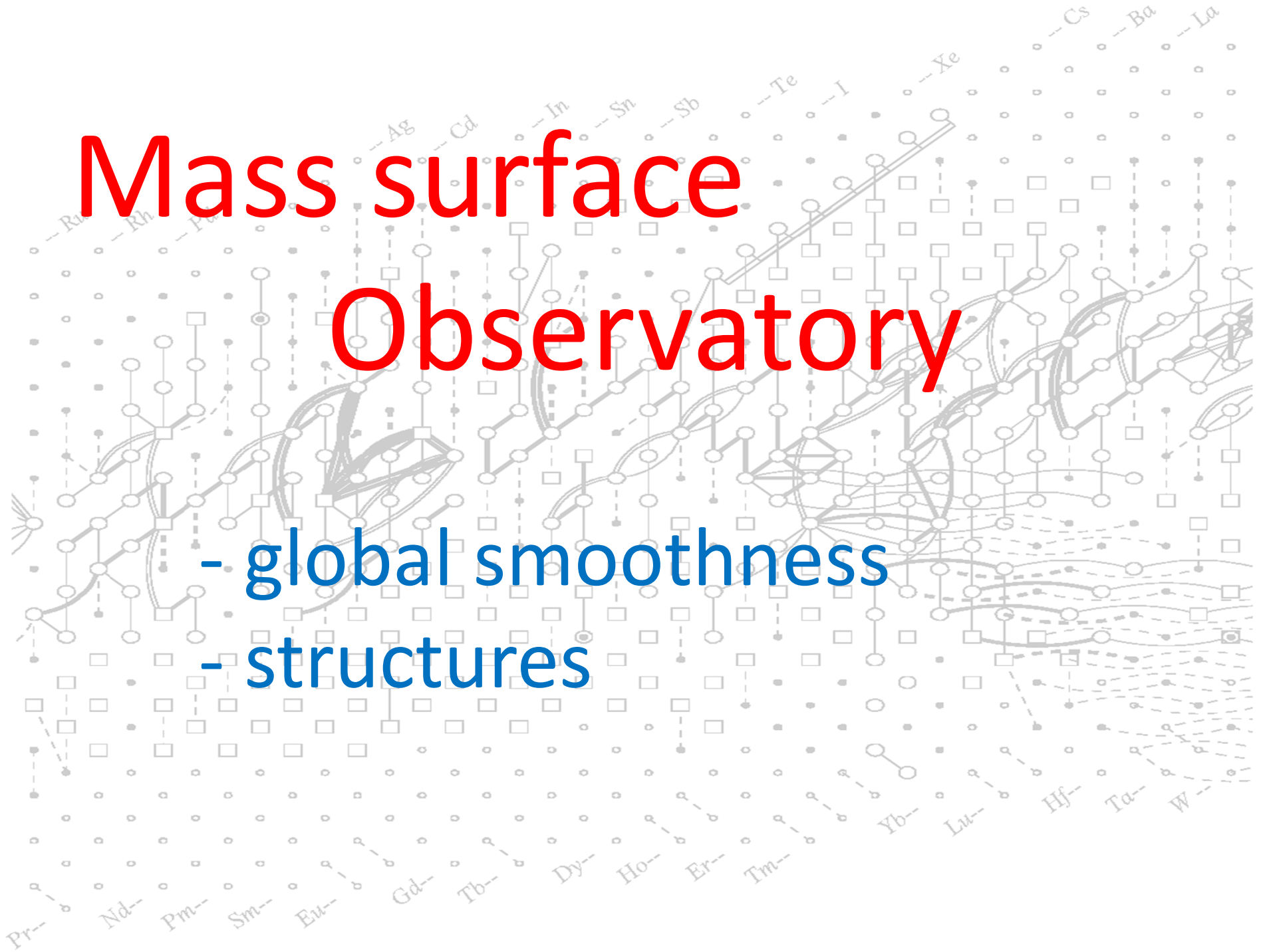
masses

Amount of work: reference per year



Mass surface Observatory

- global smoothness
- structures



The Ame (“Atomic Mass Evaluation”)

- Regularity of the mass-surface

Smoothness and structures

Surface in 3D space

Structures on the Surface: Shells - Deformations - Wigner

Regularity is a basic property of the surface of masses

Consequences :

New Physics

Outliers

Conflict among Data

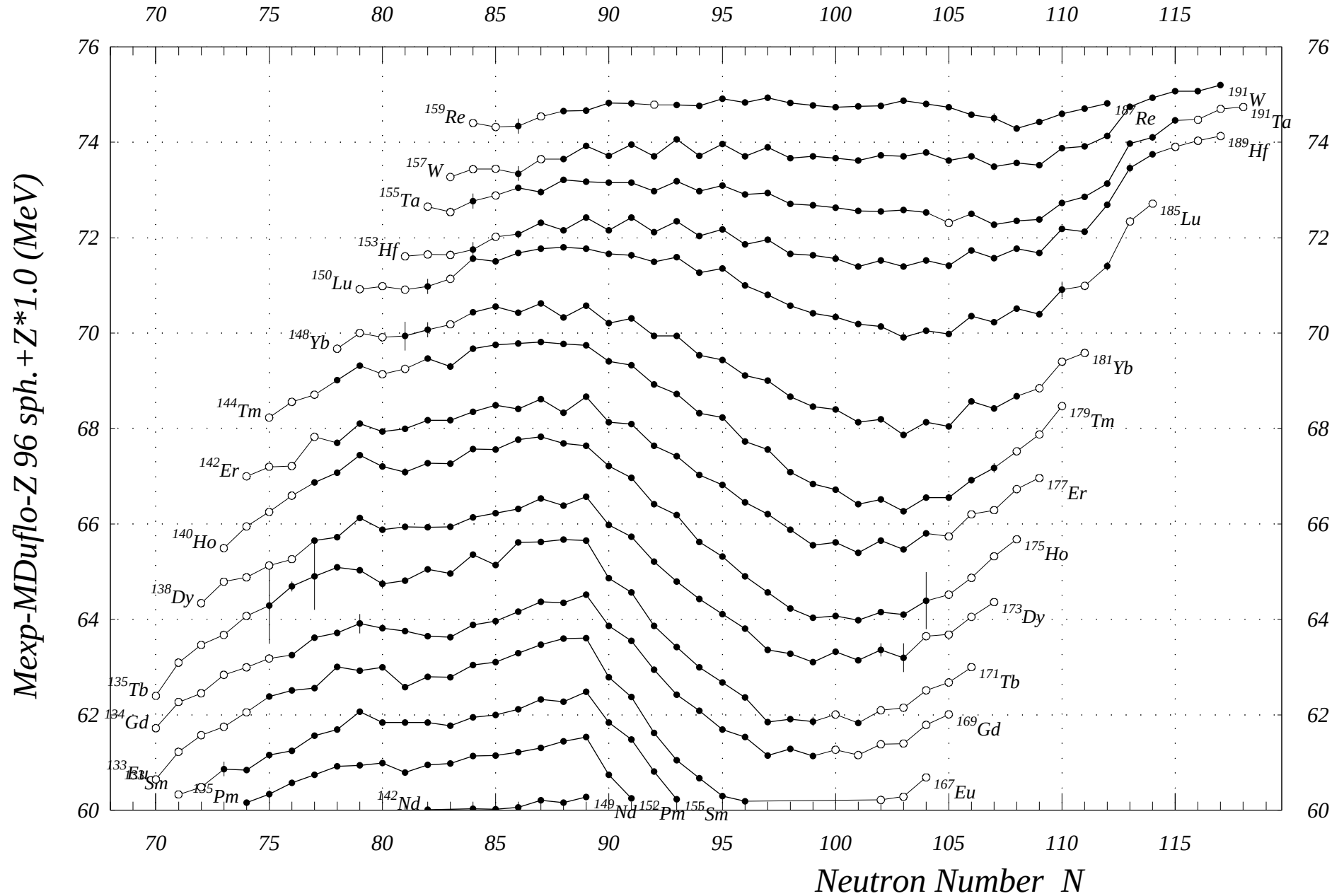
Estimate unknown masses

Regularity of the Mass Surface II

- New Physics
 - Coherent deviations in (N, Z)
 $\Rightarrow$ new physical property (e.g. $^{23}\text{N}_{15}$ $N = 108 - 115$ Cs_{63-112})
- Outliers
 - One single 'Irregularity'
 $\Rightarrow$ question correctness of datum
re-measure same and/or measure neighbors
strongly deviating 1-experiment (chaotic surf.):
 $\Rightarrow$ replace by estimated 'recommended' value
- Conflict among Data
 $\Rightarrow$ which one agrees with estimate?
- Unknown Masses
 $\Rightarrow$ Estimates: Interpolate - Extrapolate

Fig. 6. Mass Exp-Mass Duflo-Z 96 sph. N= 70 to 118

s 17 nov 2012
o0p4gqdq (nov12)
Borcea-Audi



Recent observations of the mass surface

- Magic numbers vanishing (quenching)
when going far from stability
earlier : $N = 20$, $N = 28$
now also (since Ame2003) : $N = 50$, $N = 82$
- Rising of the wings
 Q_β 's often underestimated
r-process paths less far from stability
expected influence on reactors and on waste calculations

Fig. 2. Mass Exp-Mass Duflo-Z 96 sph. $N=$ 8 to 46

s 17 nov 2012
o0p4gqdq (nov12)
Borcea-Audi

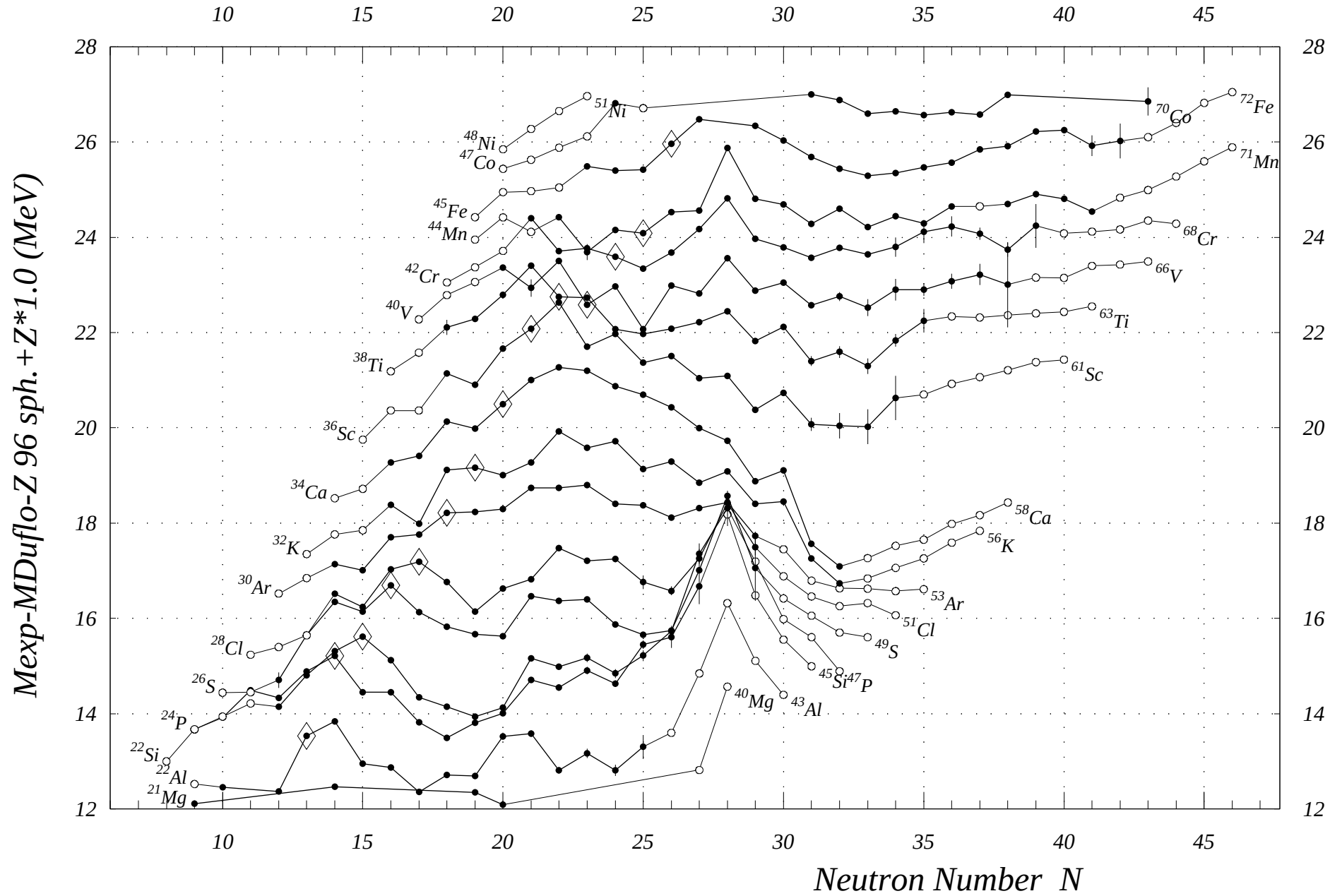


Fig. 3. Mass Exp-Mass Duflo-Z 96 sph. $N=$ 18 to 66

s 17 nov 2012
o0p4ggdq (nov12)
Borcea-Audi

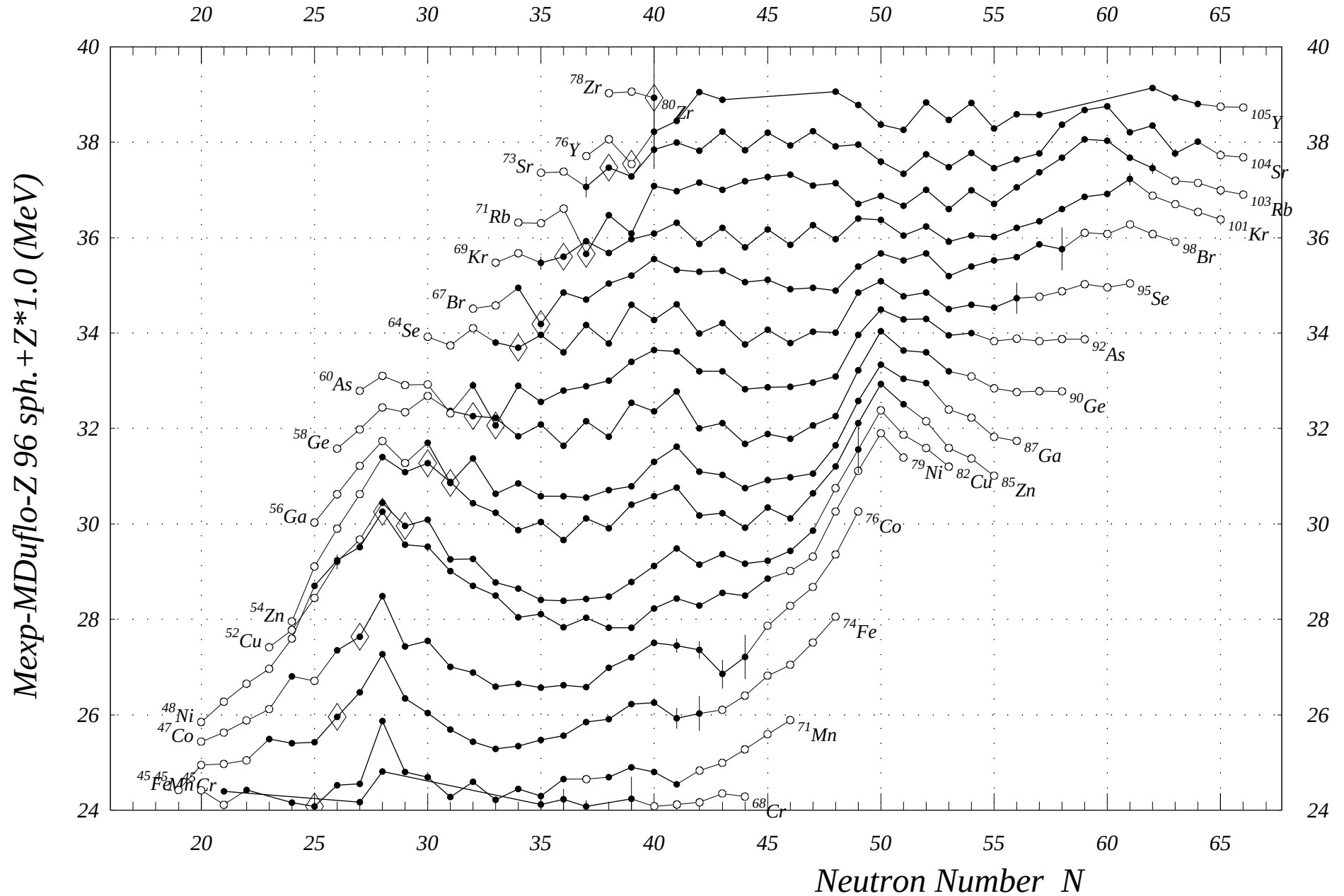


Fig. 4. Mass Exp-Mass Duflo-Z 96 sph. N= 34 to 86

d 16 nov 2003
o0p4sqyz (nov03)
Barcea-Audi

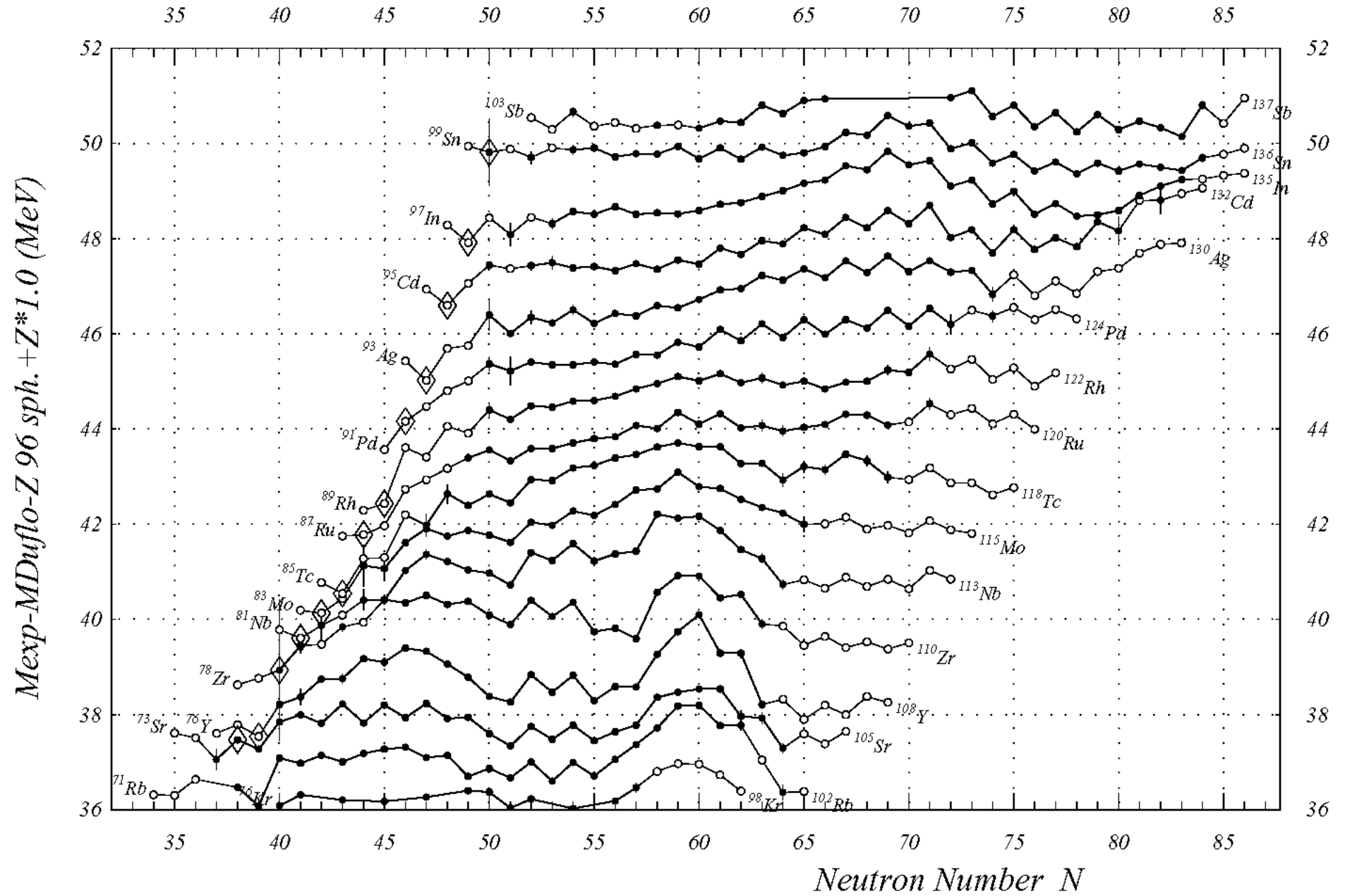


Fig. 4. Mass Exp-Mass Duflo-Z 96 sph. N= 34 to 86

s 17 nov 2012
oOp4gqdq (nov12)
Borcea-Audi

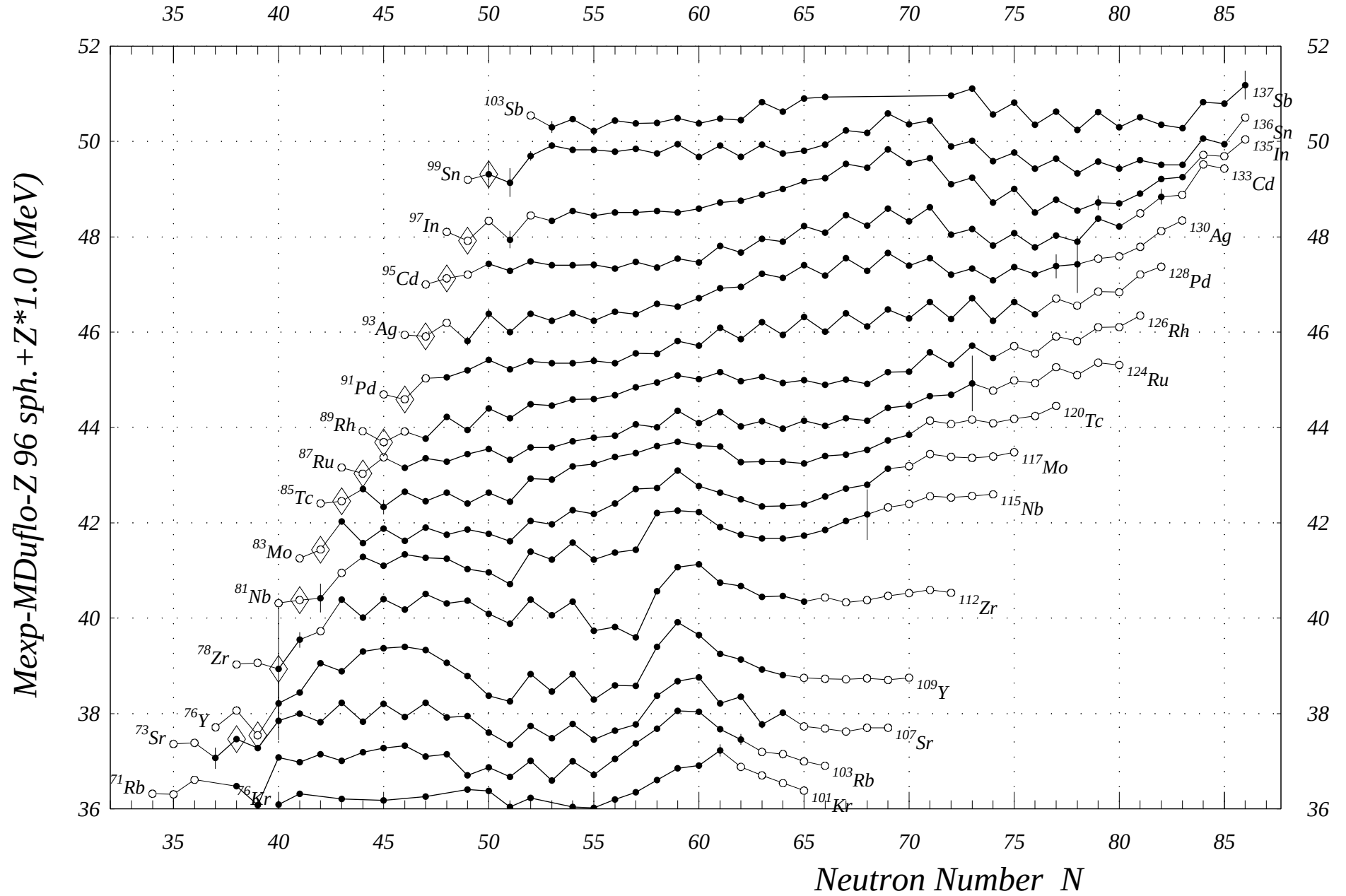


Fig. 24. α -decay energies

$N = 122 \text{ to } 145$

s 17 nov 2012
oP4gqdq (nov12)
Borcea-Audi

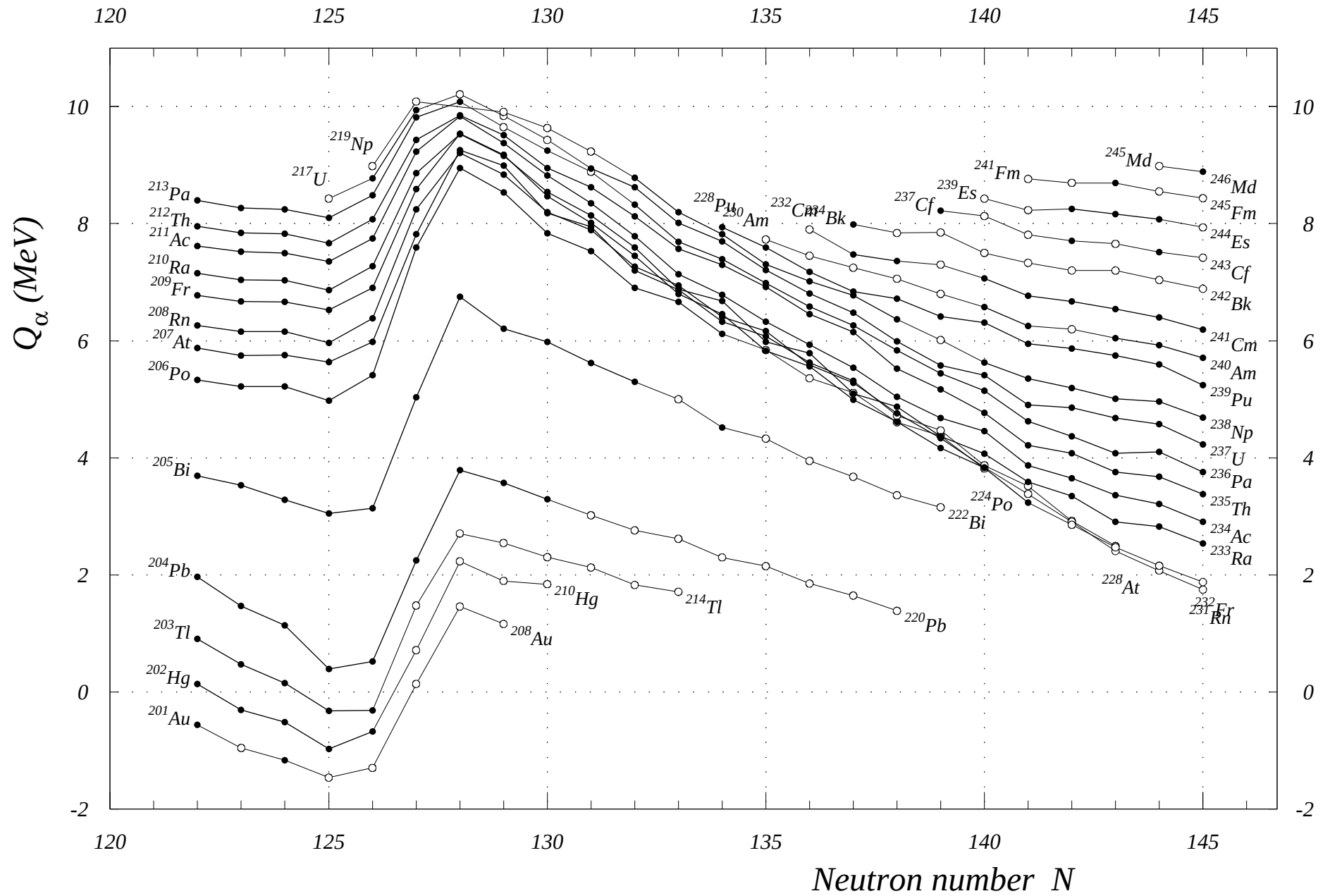
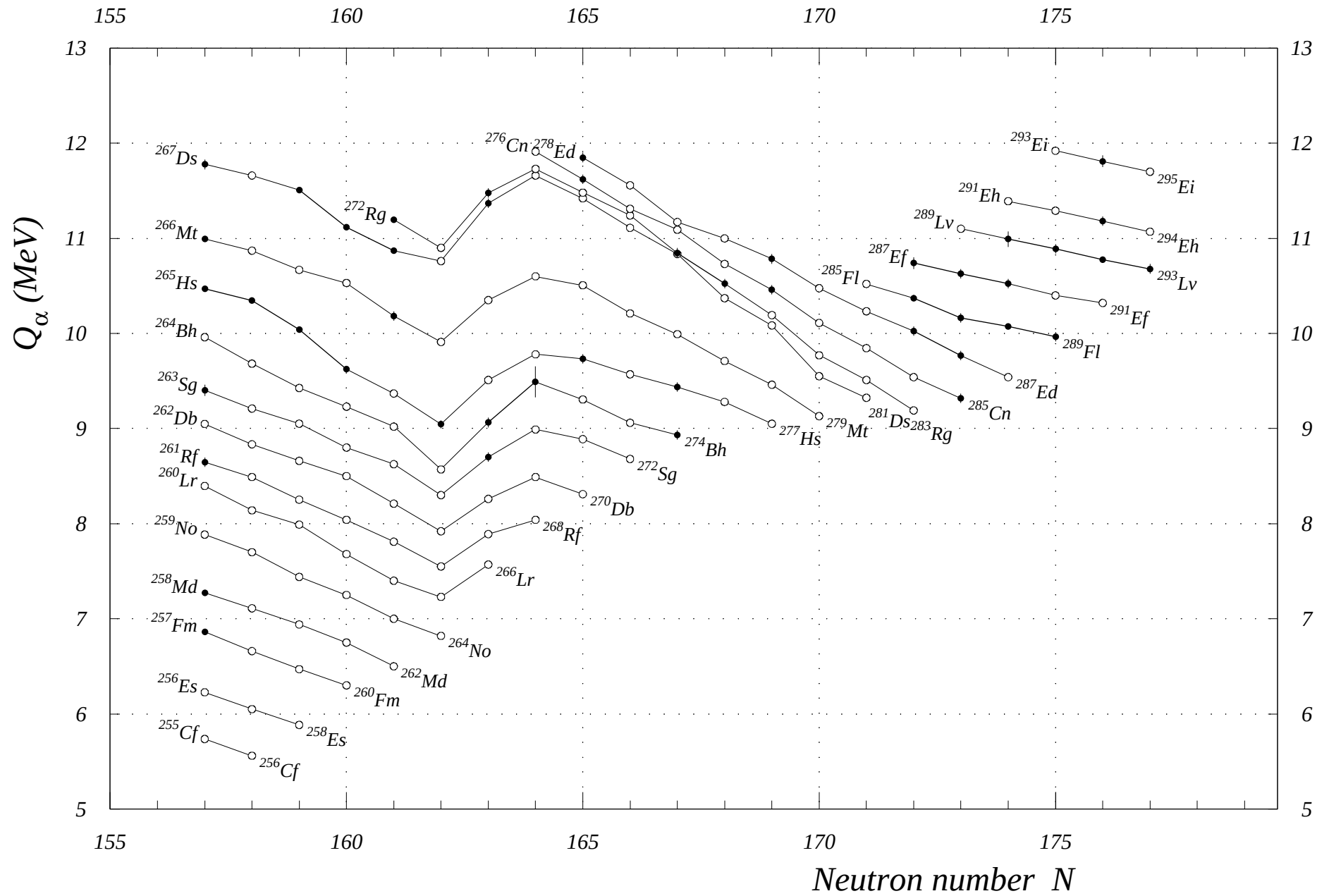


Fig. 26. α -decay energies

$N = 157$ to 178

s 17 nov 2012
o0p4gqdq (nov12)
Borcea-Audi



Conclusions

- the experimental AME (Wapstra's) is still alive
- next Tables December 2016
- new challenges (correlations)
- need to improve predictions

Thank you for your attention!

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S. Naimi, X. Xu

