

$n + {}^{235}\text{U}$ Resonance Parameters and Neutrons Multiplicities in the Energy Region below 100 eV

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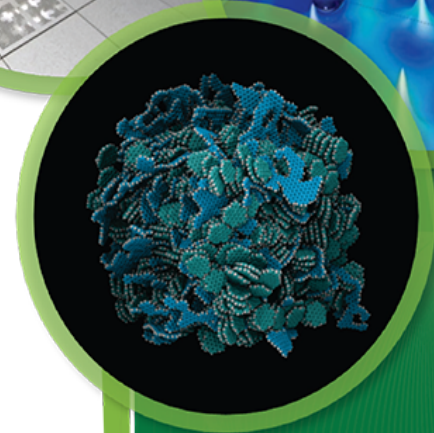
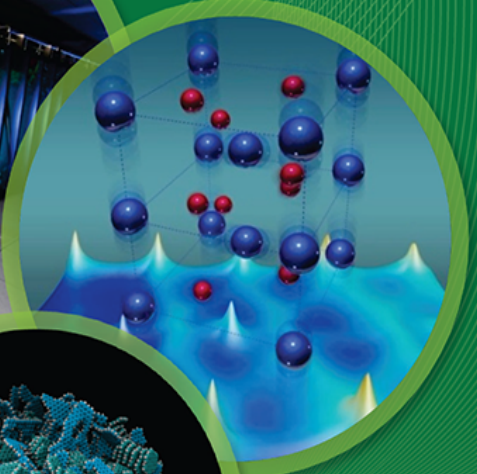
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ND2016 - Evaluation session

Bruges, Belgium, September 2016



Outline

- Introduction : motivation and background
- Nuclear data evaluation overview for ^{235}U
- Brief description of the evaluation procedure with SAMMY
 - Evaluation procedure (SAMMY algorithm)
 - Experimental data (energy-depedent cross sections, angular distributions, . . .)
 - Link to benchmarks (integral data)
- Work on $n+^{235}\text{U}$ cross sections (results)
- Summary and conclusions
- Acknowledgments

Introduction

Motivation

- For nuclear criticality applications and many others, the existing evaluated data perform well in transport simulations partly owing to *compensating errors* in the nuclear data libraries
- CIELO collaboration provides a framework for nuclear data evaluation aimed to establish the highest fidelity general purpose nuclear database
- ^{235}U among ^1H , ^{16}O , ^{56}Fe , ^{238}U , ^{239}Pu is one of the highest priority isotopes

Background

- Current status of ^{235}U evaluation in ENDF/B-VII.1 library (2011)
 - Resonance parameters are the same as ENDF/B-VI.8 release (ORNL/TM-13516)¹
 - Description of the ^{235}U resonance evaluation can be found in NEA/WPEC-18
- ^{235}U ORNL resonance evaluation(=CIELOb18=023) is part of the ENDF/B-VIII.0β2 release (2016)

¹See also L. C. Leal, H. Derrien, N. M. Larson, R. Q. Wright, *Nucl. Sci. Eng.*, **131** 230 (1999).

Nuclear Data ORNL Evaluation Overview

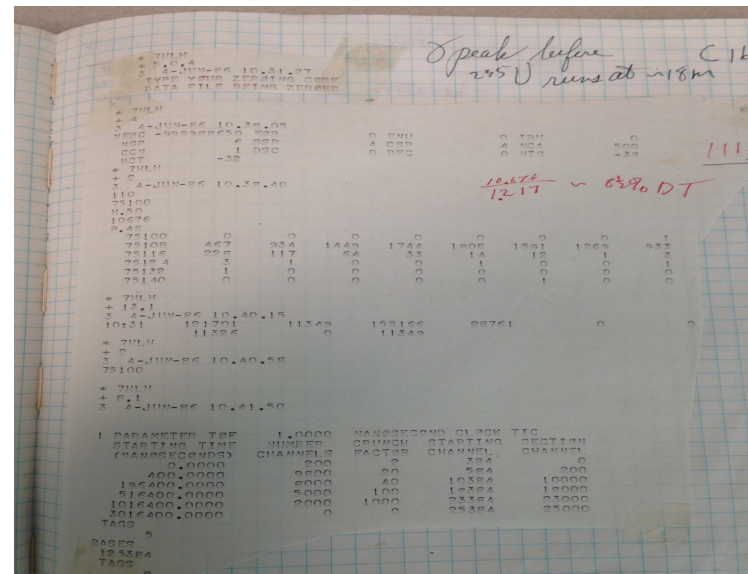
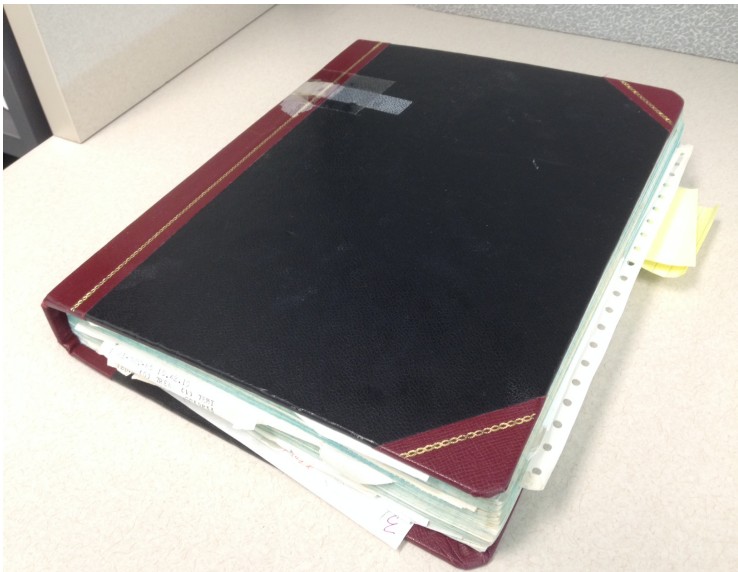
Resolved Resonance Region (RRR) Cross Section Evaluations

| No. | Nucleus (I^π) | $E_{\min} - E_{\max}$ | Method | No. Levels | J_{3-} | J_{4-} | Evaluator |
|-----|--------------------------------------|-------------------------------|-------------|------------|----------|----------|-----------|
| 1 | ^{235}U (7/2 ⁻) | 10 ⁻⁵ eV– 2.25 keV | Reich-Moore | 3164 | 1433 | 1731 | Pigni |

- The current ORNL resonance evaluation **o23** (ORNLv23) is an intermediate step of the evaluation process within CIELO
- The current **o23** resonance evaluation started from a set of resonance parameters (**o17**)
 - **o17** was documented in the ORNL presentation at the mini-CSEWG meeting (LANL, April 2016) and released in May 2016 as part of the ENDF/VIII.0 β 1 release.
- Particular emphasis in producing **o23** was devoted to
 - *Sub-thermal and thermal* : Thermal Constants (Pronyaev, micro. data)
 - *Fission integrals* (7.8-11 eV)
 - Neutron incident energies up to 20 eV for *measurements of $\alpha = \sigma_\gamma / \sigma_f$ (or η)*

Nuclear Data ORNL Evaluation Overview

- The current ORNL resonance evaluation **o23** is generated by the SAMMY code using the *Reich-Moore approximation*
 - All SAMMY inputs included in the current evaluation procedure are written using the most recent key-word for particle-pair definitions.
 - Isotopic impurities included
 - Parameters for the resolution functions (crunch data, γ -peak) of transmission experimental data (J. A. Harvey) retrieved from ORELA logbook (special thanks to K. Gu-ber).
- Residuals and chi-squared of all experimental data



SAMMY Algorithm

The various reaction cross sections $\sigma_{cc'}$ for an incoming channel c and outgoing channel c' can be written in terms of the matrix

$$X_{cc'} = \sqrt{P_c} L_c^{-1} \sum_{c''} [(L^{-1} - R)^{-1}]_{cc''} R_{c''c'} \sqrt{P_{c'}} \delta_{JJ'}, \quad (1)$$

where, in the eliminated-channel approximation, the matrix R (or R -matrix) for the channel spin group defined by the total spin J^π is

$$R_{cc'} = \left[\sum_{\lambda=1}^n \frac{\gamma_{\lambda c} \gamma_{\lambda c'}}{E_\lambda - E - i\bar{\Gamma}_{\lambda\gamma}/2} + R_c^{\text{ext}} \delta_{cc'} \right] \delta_{JJ'} \quad (2)$$

SAMMY derives from the best fit of experimental data the reduced-width amplitude $\gamma_{\lambda c}$ related to the channel width using

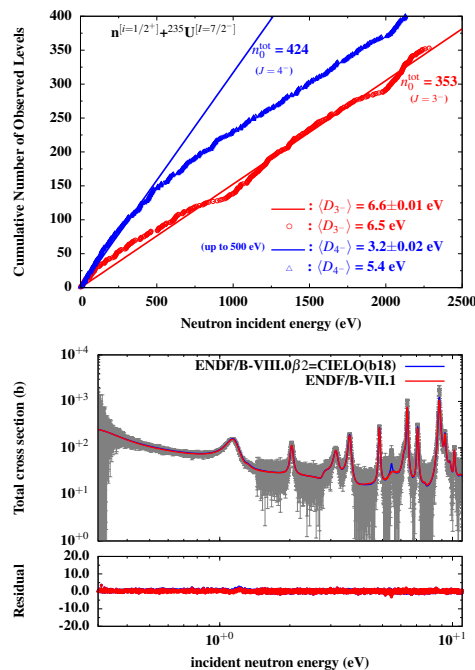
$$\Gamma_{\lambda c} = 2\gamma_{\lambda c}^2 P_c(E), \quad (3)$$

where the penetrability factors depend on the Coulomb functions F_ℓ , G_ℓ as $P_c(E) = ka/[F_\ell^2(ka, \eta) + G_\ell^2(ka, \eta)]$.

Differential and Integral Data

Differential data

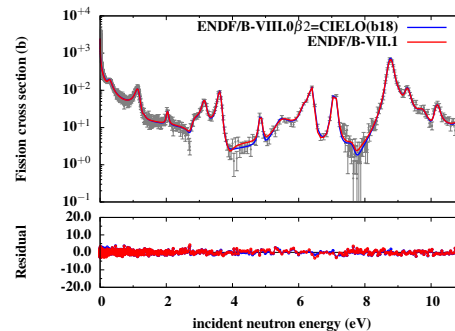
- Application of the *R*-matrix SAMMY method (Reich-Moore) to determine a consistent set of neutron resonance parameters (RP) based on the fit of available experimental data (transmission, capture, angular distribution, ...)
- Statistical properties of RP such as average spacing $\langle D_\ell \rangle$ and strength function S_ℓ



Integral data

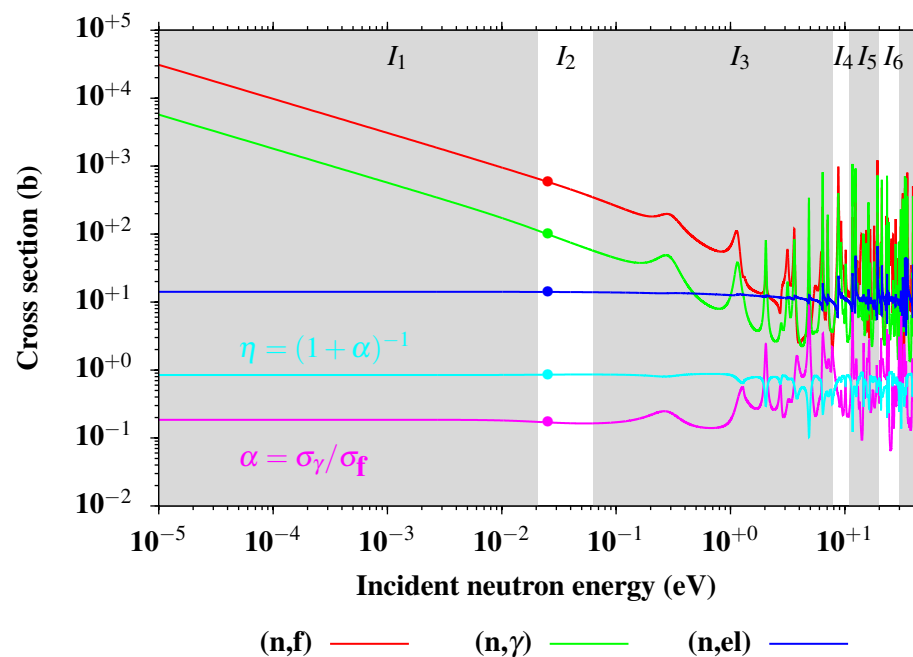
- Resonance parameter and covariance are converted into the ENDF/B format - file 2 (parameter) and 32 (covariance matrix)
- Process ENDF/B file with processing codes as NJOY or AMPX in order to generate cross section in point-wise and/or group representation
- Test evaluations against integral benchmarks (e.g. reaction rate) sensitive to a specific energy range (RRR)

$$R = \int_{RRR} \sigma(E) \phi(E) dE \quad (4)$$



Thermal Cross Sections and Integrals

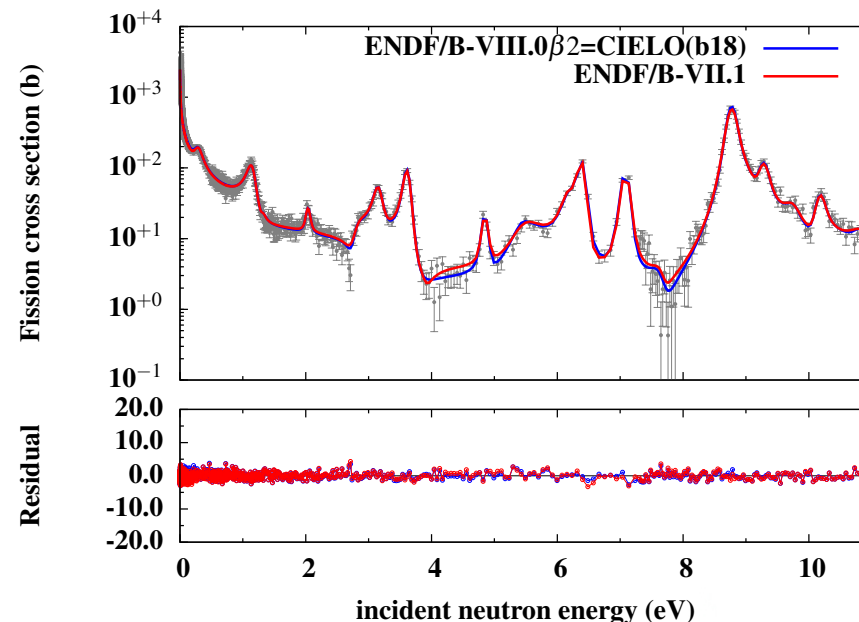
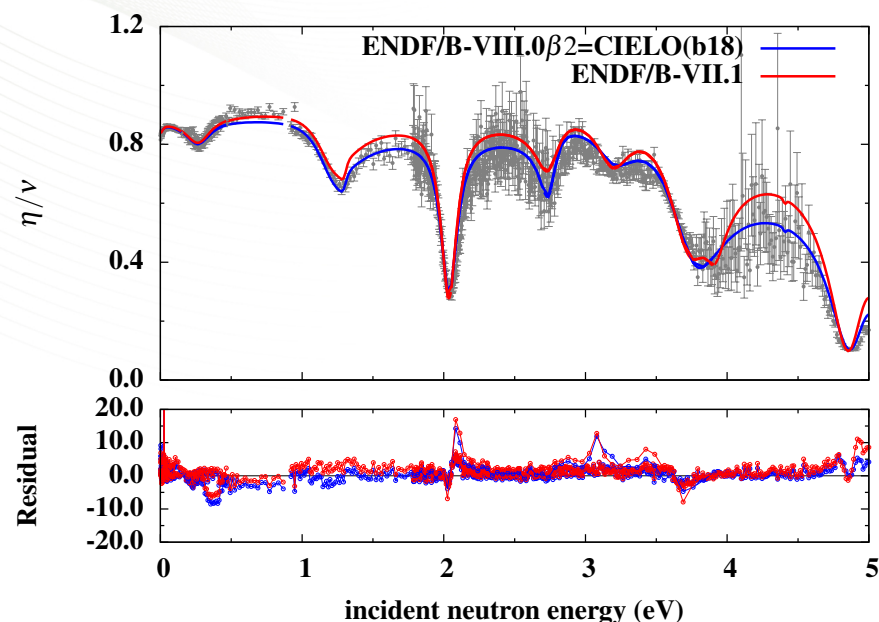
- **o23** values for fission and capture thermal cross sections are based on $^{235}\text{U}(n,f)$ thermal constants obtained on the basis of microscopic data (i.e., only considering Wallner thermal capture measurements)
- Fission integral (I_4 in the Figure below) between 7.8 and 11 eV based on recommendation of Neutron Standards



Thermal values

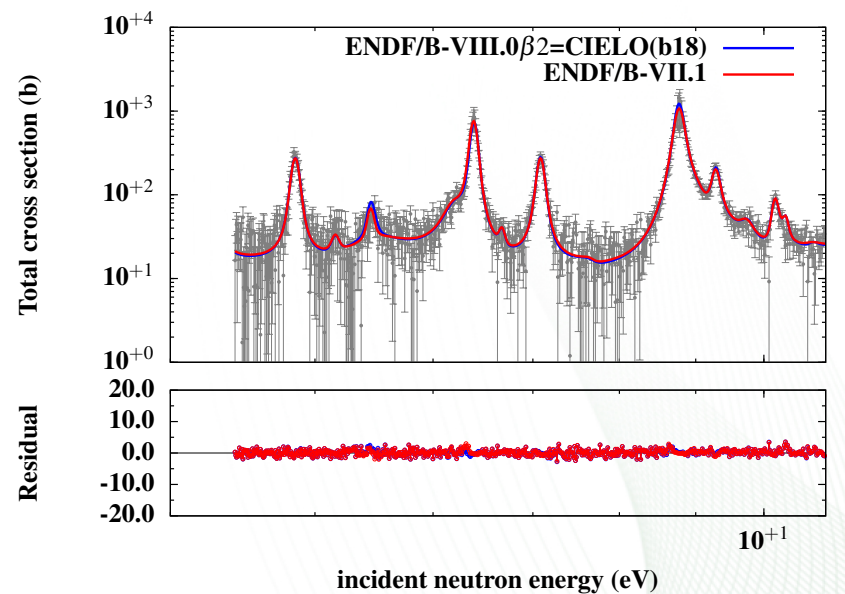
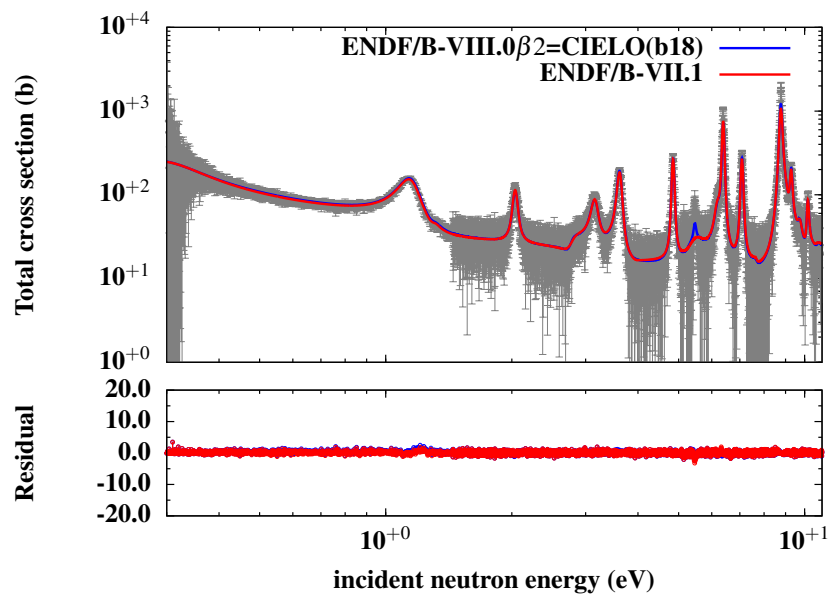
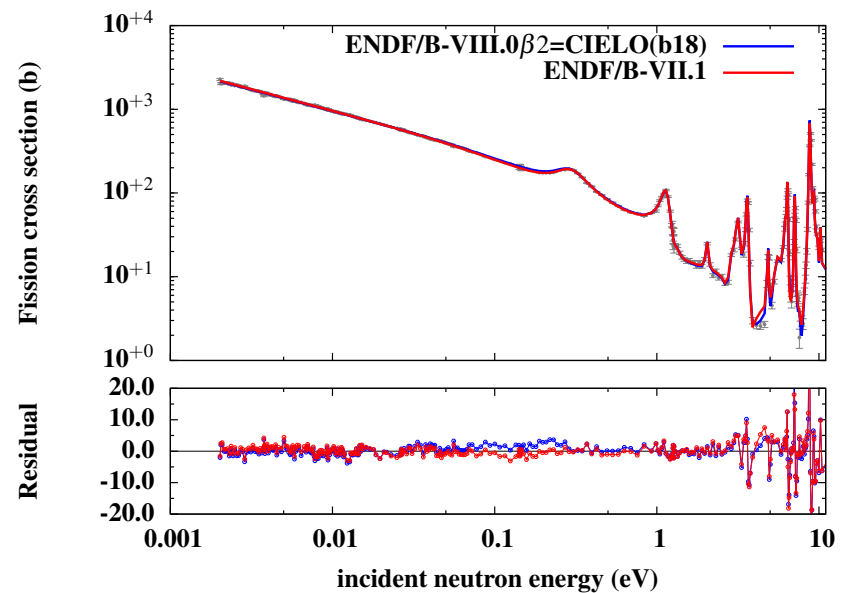
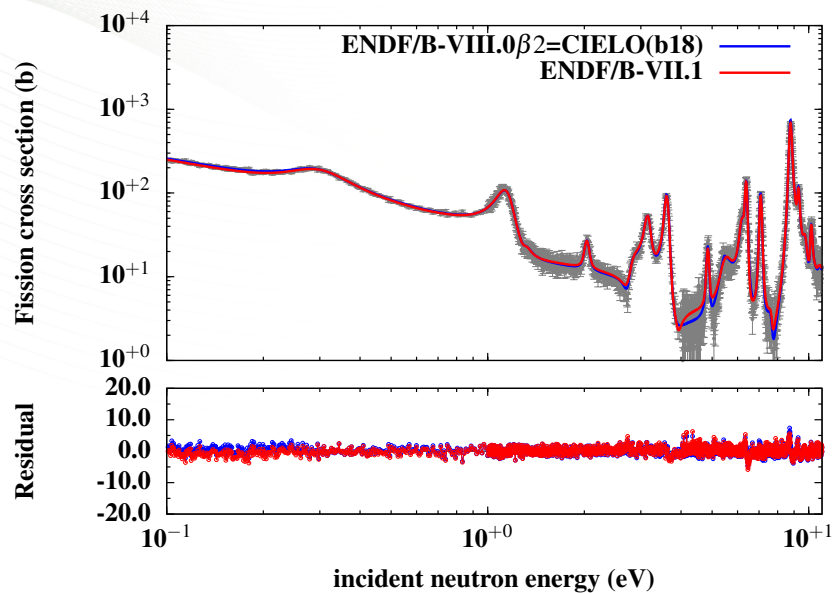
| Standards | o23 (T=0° K) | |
|-------------|--------------|-----------|
| 587.15±1.36 | 586.6 | (n,f) |
| 99.26±2.03 | 99.4 | (n,gamma) |
| 14.09±0.21 | 14.08 | (n,el) |
| 0.855 | 0.855 | η |
| 0.1690 | 0.1694 | α |

Results



- $n+^{235}\text{U}$ η measurements of Brooks, Wartena, and Weigmann (left) and Gwin's fission measured cross sections (right) compared to ENDF/B-VII.1 and ENDF/B-VIII.0 β_2 values.
- the CIELO η (decreased) values are, on average, in better agreement with the experimental data
 - achieved by increasing the capture cross sections, mostly in the valley of the resonances while keeping their peak values unchanged. The resonance at $E_n=2$ eV is clearly an example.
- The sensitivity of the resonance parameters to fission cross sections seems to be more relevant than to capture cross sections at neutron energies $\gtrsim 4$ eV (see fission cross sections shown in blue continuous line).

Other Results



Summary and Conclusions

- We applied the *R*-matrix SAMMY method using the Reich-Moore approximation to determine a consistent set of neutron resonance parameters for ^{235}U
- The **o23**=CIELOb18 is currently part of the ENDF/B-VIII.0 β 2 (2016)
- Constraints applied on the **o23** resonance parameter evaluation are
 - Brooks' η experimental data
 - Standard thermal cross sections and the fission integral between 7.8–11 eV
 - New thermal Prompt Fission Neutron Spectra (PFNS)
- The present set of resonance parameters yields cross sections still in reasonable agreement with the suite of experimental data
- The validation analysis on the thermal benchmarks showed good agreement with the experimental response and that the **o23** resonance parameters are compatible with the current values of $\bar{\nu}$ (from thermal constants) and thermal PFNS (average energy 2.00 ± 0.01)

Conclusion : new resonance analysis allowed to combine new evaluation of Thermal Neutron Constants, the recommended value of the fission resonance integral from 7.8-11 eV, new PFNS evaluation, and to describe Brooks data while keeping an excellent agreement with existing fission, capture and transmission measurements.

Future Work : Analysis of new experimental data (fission and capture) over the entire energy range up 2.25 keV.

Acknowledgments

This work was supported by the US Department of Energy (DOE), Nuclear Criticality Safety Program (NCSP) funded and managed by the National Nuclear Security Administration for DOE.

Thank you!