

Covariances for the ^{56}Fe radiation damage cross sections

S.P. Simakov, A. Koning*, A.Yu. Konobeyev

*) Nuclear Data Section, IAEA, Vienna

INSTITUTE for NEUTRON PHYSICS and REACTOR TECHNOLOGY (INR)



Objectives of the present work:

- evaluation of covariance matrices for Physical Quantities used for characterization of neutron induced Radiation Damage in Materials
- They include:
 - kinetic energy released by ch.particles *KERMA* - locally deposited Nuclear Heating
 - damage energy *DE* - defines the number of displaced atoms $dpa = 0.8 \cdot DE / E_d$
 - gas production (n, xHe) , (n, xT) , (n, xH) ... - transmuting target nuclei into gases
- Such Uncertainties and Energy-Energy or Reaction-Reaction correlations **were not assessed so far**, whereas the covariances for many cross sections are often presented in modern evaluated data libraries
- Since damage quantities depend on many reactions channels and energy-angular distributions of reaction recoils, the evaluation of uncertainty is not straightforward
- To reach a declared goal, we used an idea of Total Monte Carlo (*TMC*) application to Nuclear Data

This study was stimulated by:

IAEA Coordinated Research Project “Primary Radiation Damage Cross Sections”

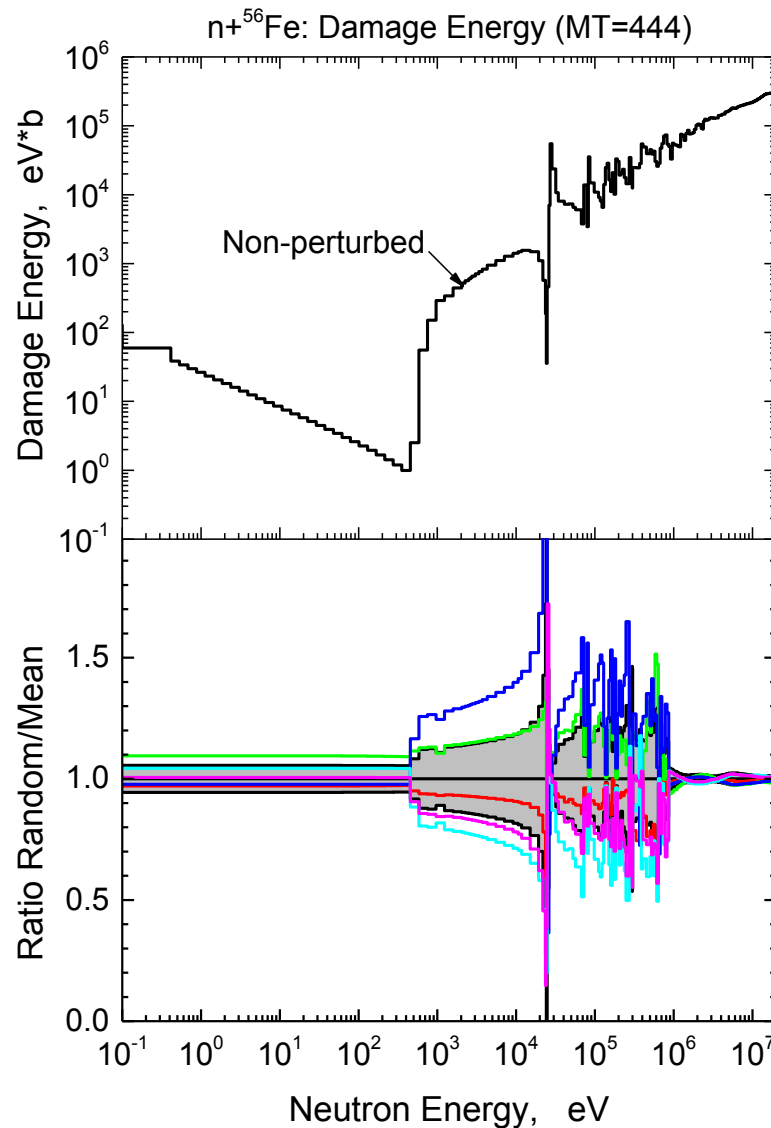
(<https://www-nds.iaea.org/CRPdpa/> or just google “IAEA dpa”)

Method of calculation of Energy-Energy and Reaction-Reaction Covariancies from TENDL random files by TMC



- we used 1 unperturbed (original, < 200 MeV) and 500 random (sampled input parameters of nuclear model, < 20MeV) files for $n + {}^{56}\text{Fe}$ from TENDL-2013
- all 501 files were processed by NJOY-2012.50+ to get needed physical quantities as ENDF-6 formatted files. Following NJOY modules (additionally to RECONR, BROADR [T = 293K], ...) were used:
 - HEATR - to calculate KERMA (energy balance designed by MT = 301) and Damage Energy (MT = 444)
 - GASPR - to calculate gas production cross sections $(n, x^4\text{He}) = \text{MT207}$, $(n, x^3\text{He}) = \text{MT206}$, $(n, xt) = \text{MT205}$, $(n, xd) = \text{MT 204}$ and $(n, xp) = \text{MT203}$
 - GROUPR - to produce **desired quantities in grouped-wise format *gendf*** (we selected VITAMIN-J 175gr which covers 10^{-5} eV to 19.64 MeV)
- Fortan-90 code was written to read in ***gendf files*** and to calculate Energy-Energy (E-E) and reaction-reaction (MT-MT) covariance matrices and SPectra Averaged quantities (SPA)

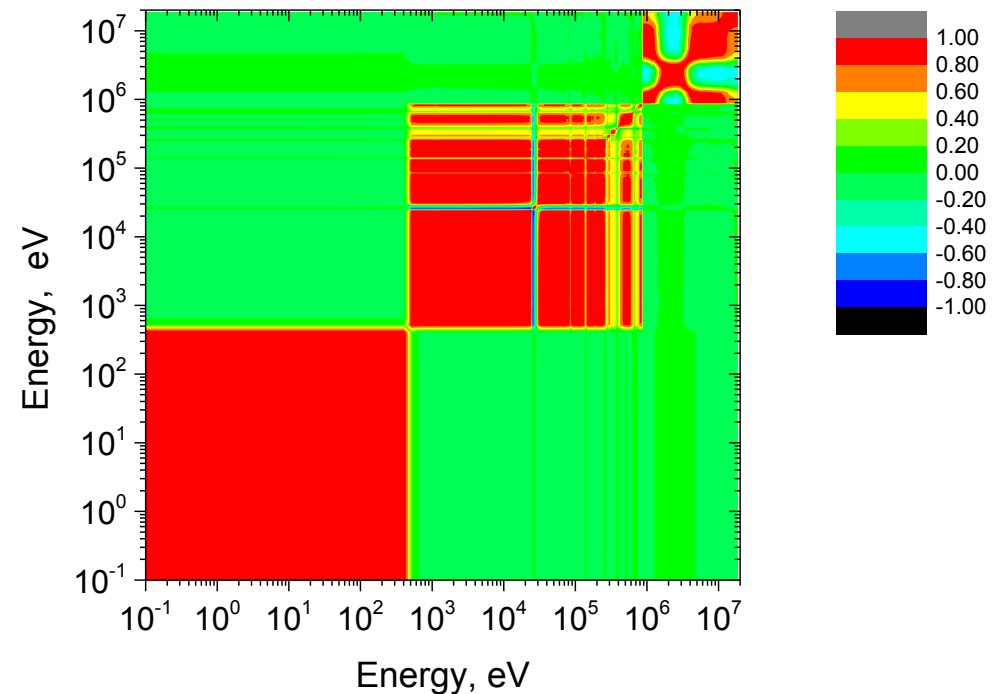
Results: Derived Covariance Matrices, example for Damage Energy (MT=444)



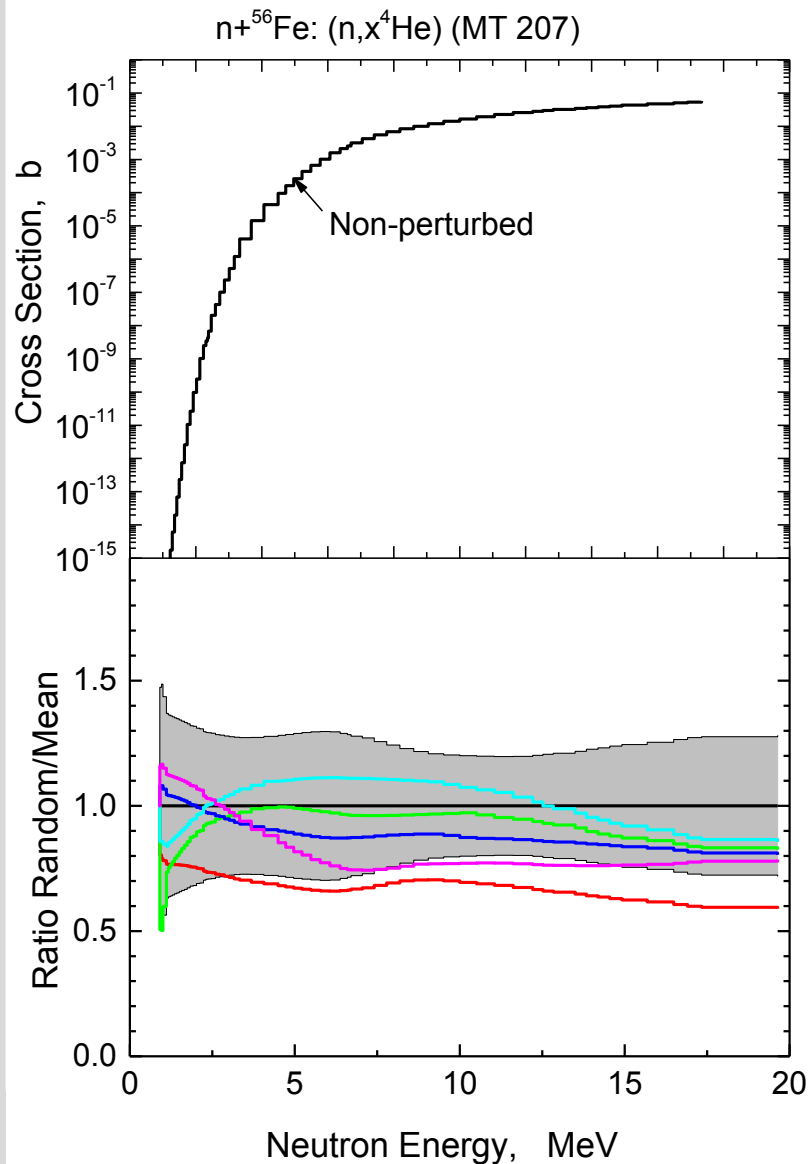
← Quantity and Uncertainties ($\approx 1-40\%$)

↓ Correlation Matrix (3 regions with ≈ 1)

Fe-56: Damage Energy (MT=444) correlation matrix
from 500 TENDL-2013 random files

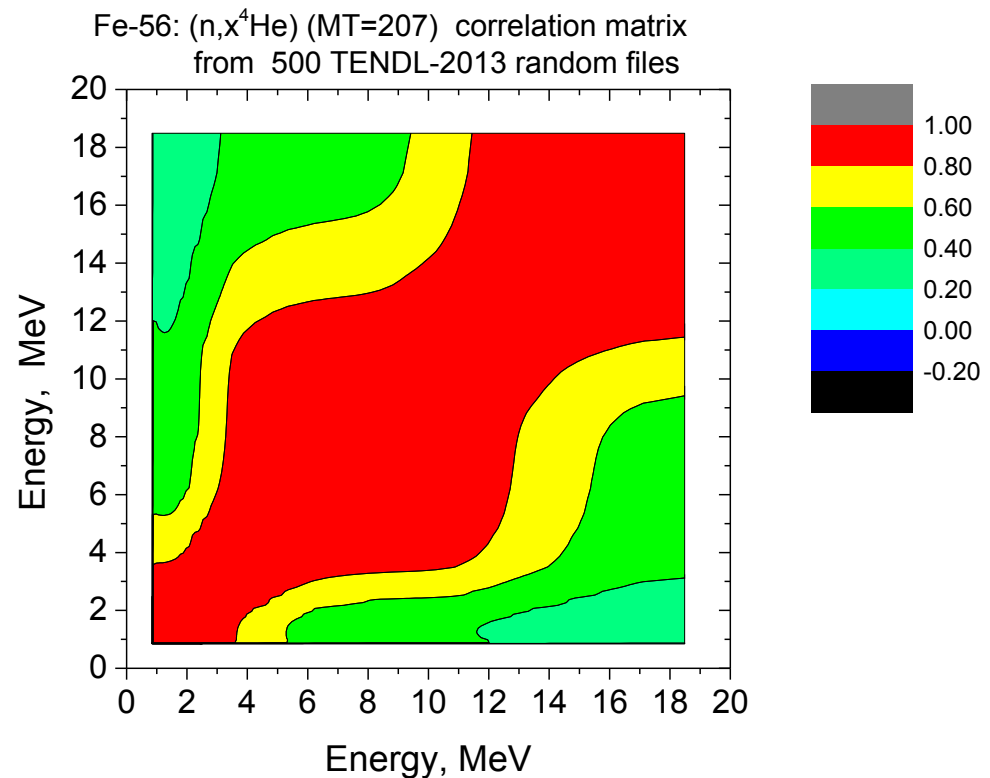


Results: Derived Covariance Matrices, example for gas production ($n, x^4\text{He}$) (MT = 207)



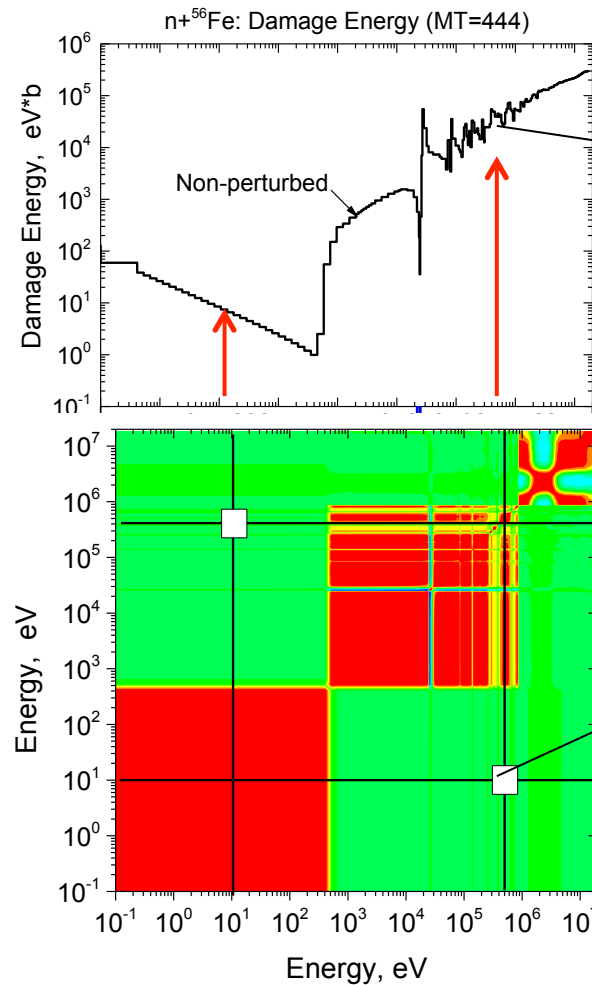
← Quantity and Uncertainties ($\approx 30\%$)

↓ Correlation Matrix
(≈ 1 within 50% energy interval)

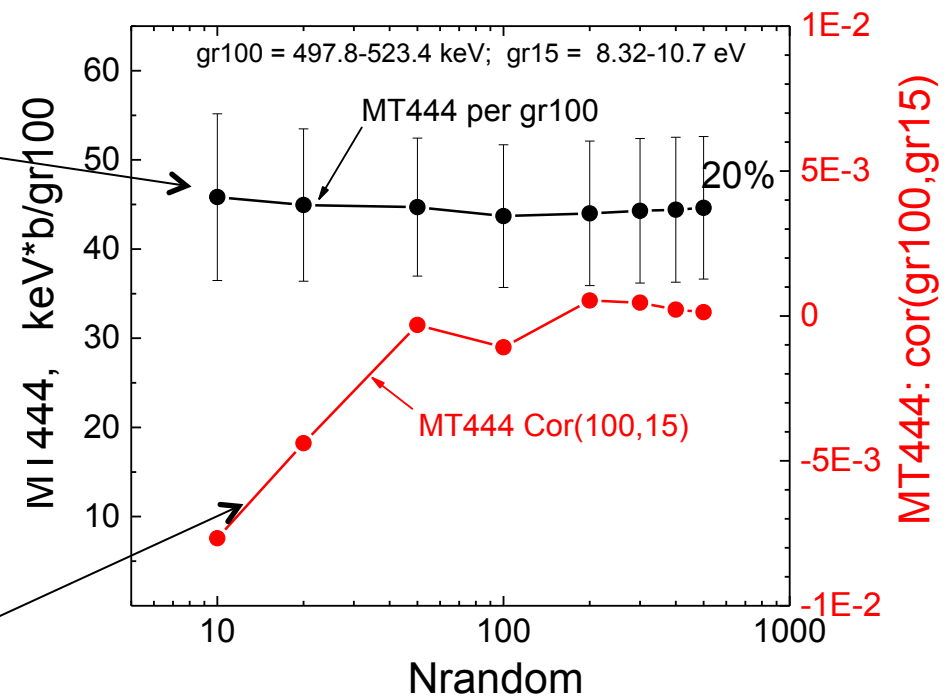


Results: Statistical Significance (Convergence) of 175gr Uncertainty and 175 x 175gr E-E Correlation Matrix, example:

MT444: $\sigma(E)$ and Cor(E,E)



MT444: $\sigma(\text{gr100})$ and Cor(100,15)



Observations:

- One group σ and $\Delta\sigma$ converge at Nrandom = 50-100
- E-E Correlation Elements converge at Nrandom \approx 200
- thus, 175 gr presentation of Cov Matrix (< 20 MeV) from 500 random files is statistically correct

Results: ENDF-6 formatted E-E and MT-MT Damage Covariances to store in evaluation file

175 gr E-E relative covariance matrices for **MT=203-444** were converted in ENDF-6 **MF33 file** (NB = 5, symmetric), *thanks to A.Konobeyev*

MF33/MT203-444 file was processed by COVEIGE code (*thanks to A.Trkov*):
small negative eigenvalues $\geq (1-6)E^{-8}$ were found
(however they always give positive variances in facility spectra considered)

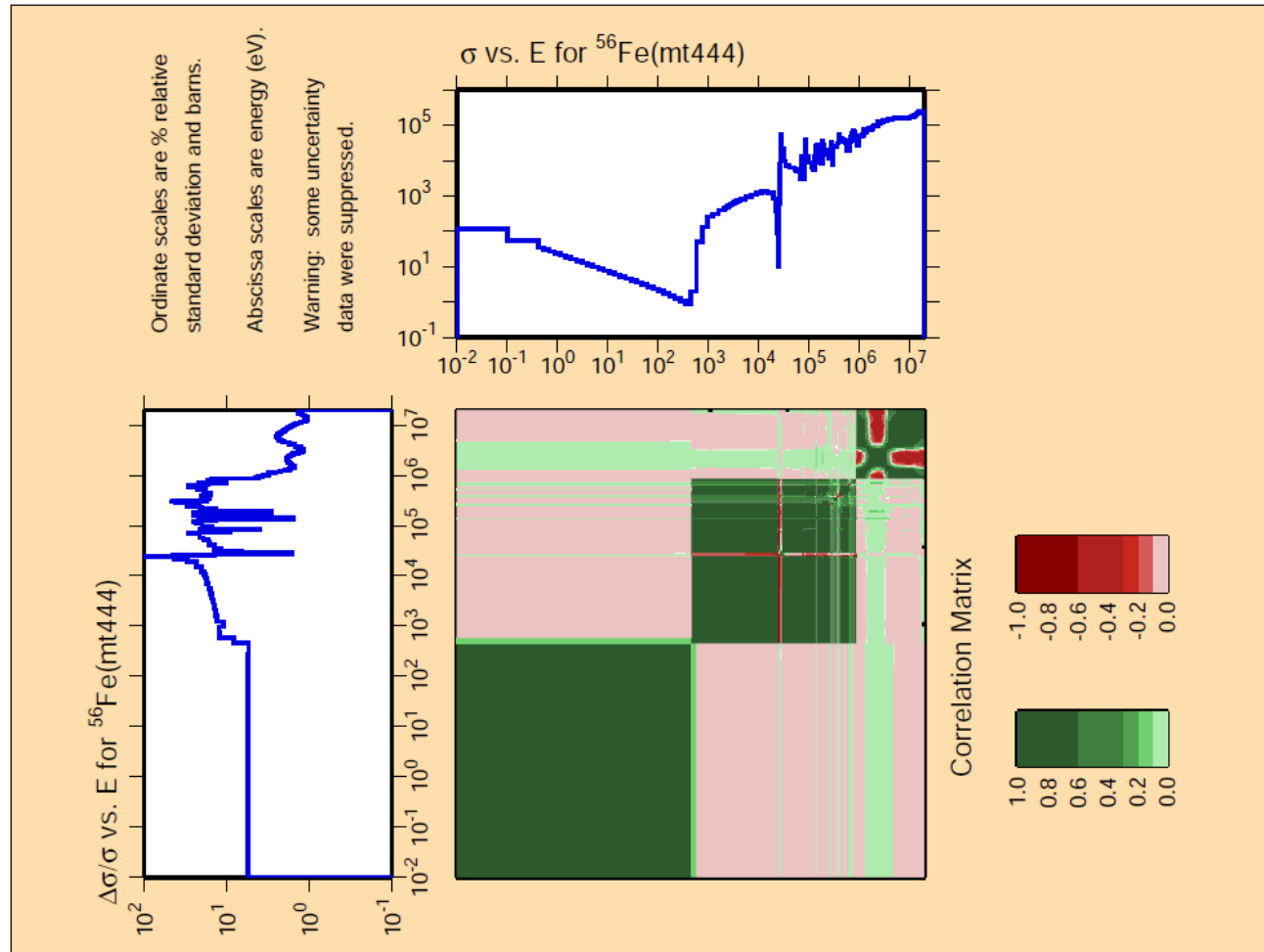
MF33MT203-444 was then added to **TENDL-2013 ^{56}Fe** file for purpose of checking on myENDF (<https://www-nds.iaea.org/exfor/myendf.htm> *thanks to V. Zerkin*) by:

- CHECKR (WARNINGS: IN MF=33 MT= 203 ALLOWED IN DERIVED FILES
ERROR FOUND: SECTION 33/203 NOT IN DIRECTORY, ...)
- FIZCON (ERROR FOUND: SECTION 33/203 NOT IN INDEX,)
- STANEF (OK!)

Finally the whole file (**TENDL-2013 ^{56}Fe + MF33 with MT 203-444**) was successfully processed by NJOY-2012.50 (ERROR, COVARR)

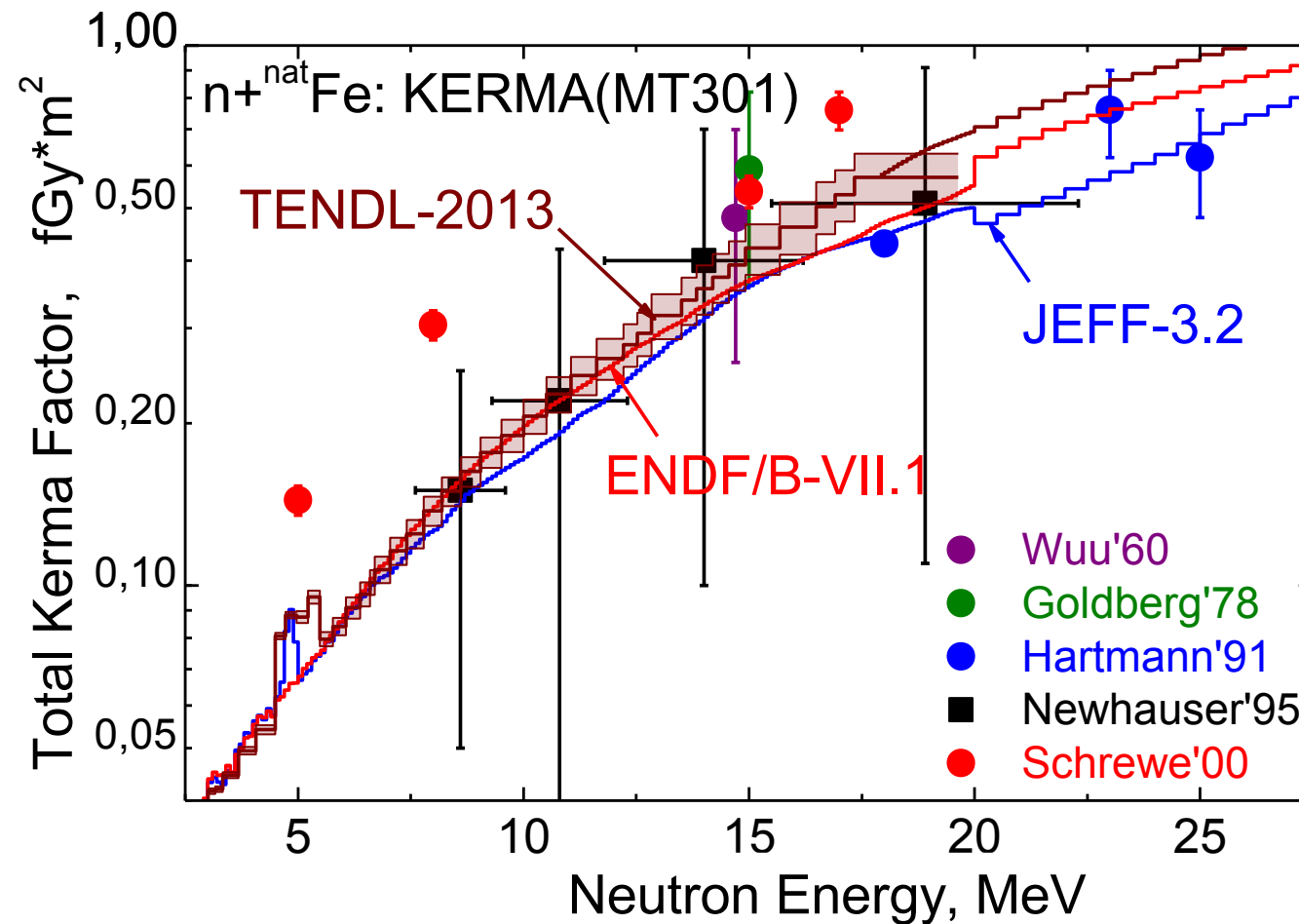
- illustrative plots on the next slide =>

Results: Damage Uncertainty and E-E Correlation in ENDF-6: plots from NJOY-2012, example for MT 444



Details noticed: NJOY automatically added ≈ 20 groups to 175gr in our MF33

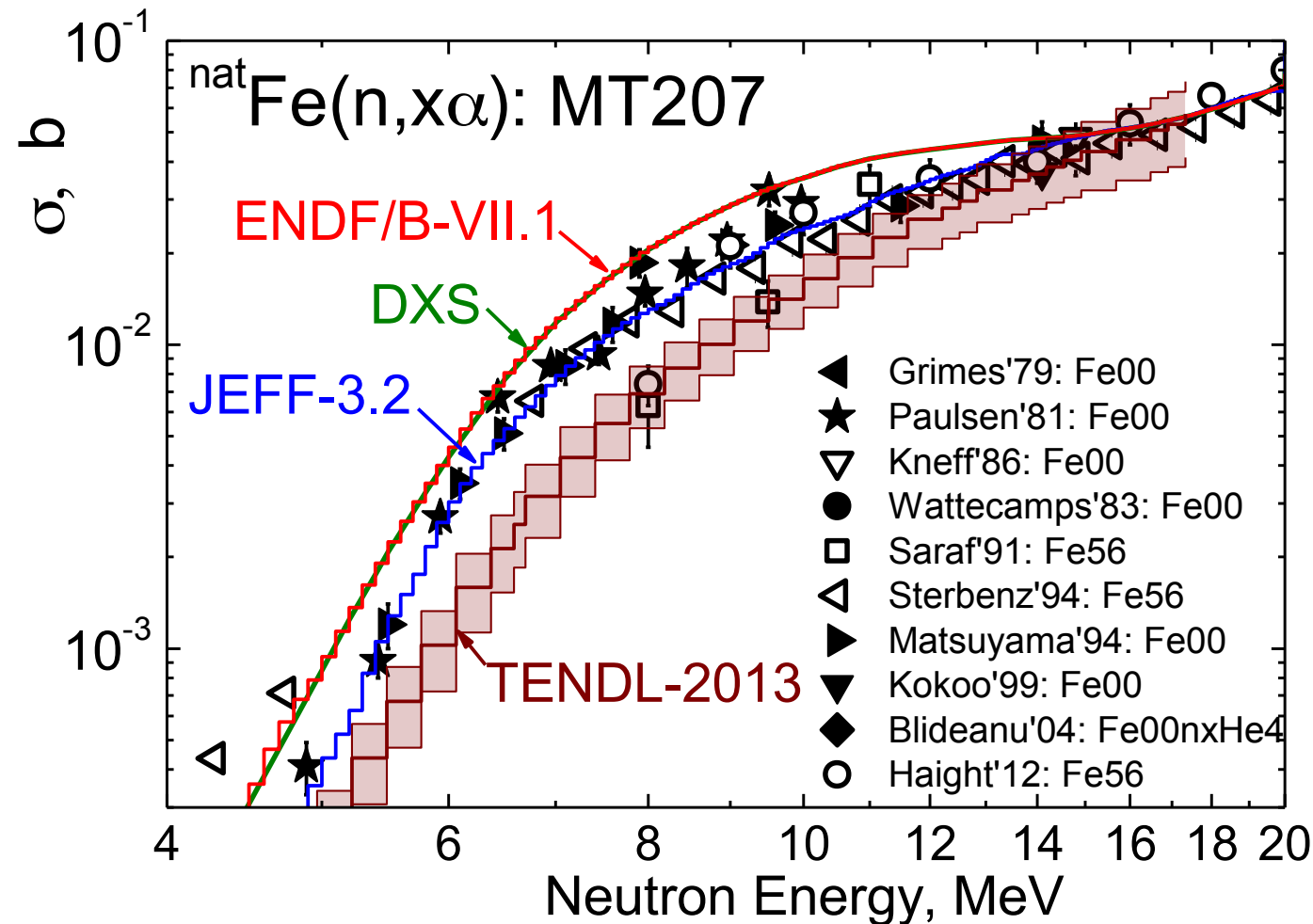
Results: Experimental Validation of Uncertainties - it is possible to do for (1): KERMA



Observations:

- Uncertainties from TENDL random files (${}^{56}\text{Fe}$, 5-10%) \leq Experimental Uncert. (6 - 100%)
- Scattering of scarce Measurements is large: **Schrewe'00 data seem have systematic error**
- **New KERMA measurements for Fe are needed ...**
- Mixing of isotopes data by MIXR/NJOY-2012 was tricky ... *(solved by O.Cabellos, A.Kahler)*

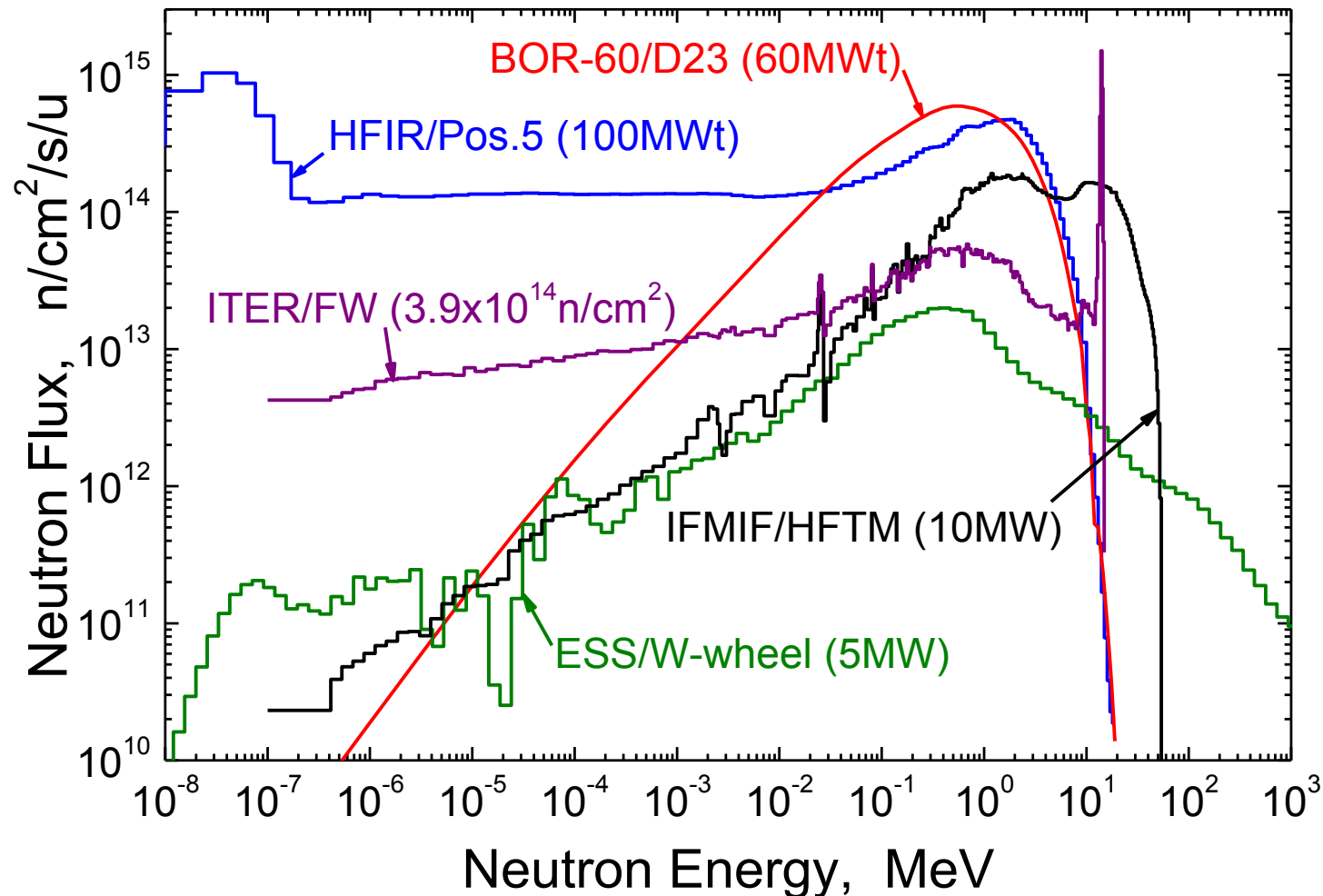
Results: Experimental Validation of Uncertainties - it is possible to do for (2): (n,x α)



Observations:

- Uncertainties from TENDL-2013 random files (^{56}Fe , 20%) \approx bulk Experimental Unc. (10-20%)
- however TENDL-2013 underestimates the mean values of cross section

Practical Applications: Spectrum Averaged (SPA) Damage and Uncertainties in Nuclear Facilities - Spectra



**For representative calculation of SPA we selected:
HFIR/C5 (Fission), ITER/FW (Fusion) & IFMIF/HFTM (Spallation)**

Practical Applications: Spectrum Averaged (SPA) Damage Uncertainties and MT-MT Corr. for HFIR, ITER & IFMIF



Bold - full E-E correlation matrix, *Italic* – ignoring off-diagonal elements

Facility/Location	HFIR/C5	ITER/FW	IFMIF/HFTM
Neutron Flux [n/cm ² /s]	5.10E+15	3.90E+14	7.32E+14
Averaged Energy [MeV]	0.41	3.47	7.00
NRT Displacements [dpa/fpy]	30.5 ± 0.95 (3.1%) <i>30.5 ± 0.24 (0.8%)</i>	10.4 ± 0.16 (1.5%) <i>10.4 ± 0.05 (0.5%)</i>	25.1 ± 0.36 (1.4%) <i>25.1 ± 0.09 (0.4%)</i>
KERMA [W/Kg]	277 ± 7 (2.7%) <i>277 ± 2 (0.7%)</i>	246 ± 21 (8.7%) <i>246 ± 12 (4.9%)</i>	469 ± 31 (6.7%) <i>469 ± 10 (2.2%)</i>
(n,x ⁴ He) [appm/fpy]	5.7 ± 1.3 (23%) <i>5.7 ± 0.3 (6%)</i>	92 ± 21 (23%) <i>92 ± 12 (13%)</i>	136 ± 31 (23%) <i>136 ± 11 (7.8%)</i>
(n,x ¹ H) [appm/fpy]	37 ± 6.3 (16.9%) <i>37 ± 1.6 (4.4%)</i>	410 ± 72 (17%) <i>410 ± 41 (10%)</i>	642 ± 102 (16%) <i>642 ± 31 (4.9%)</i>
MT-MT correlation: max. between (n,x ⁴ He) & (dpa)	204-206 = + 1.05% 207-444 = - 5.9E-5	205-206 = + 1.07% 207-444 = + 1.8E-4	204-206 = + 0.66% 207-444 = + 1.4E-4

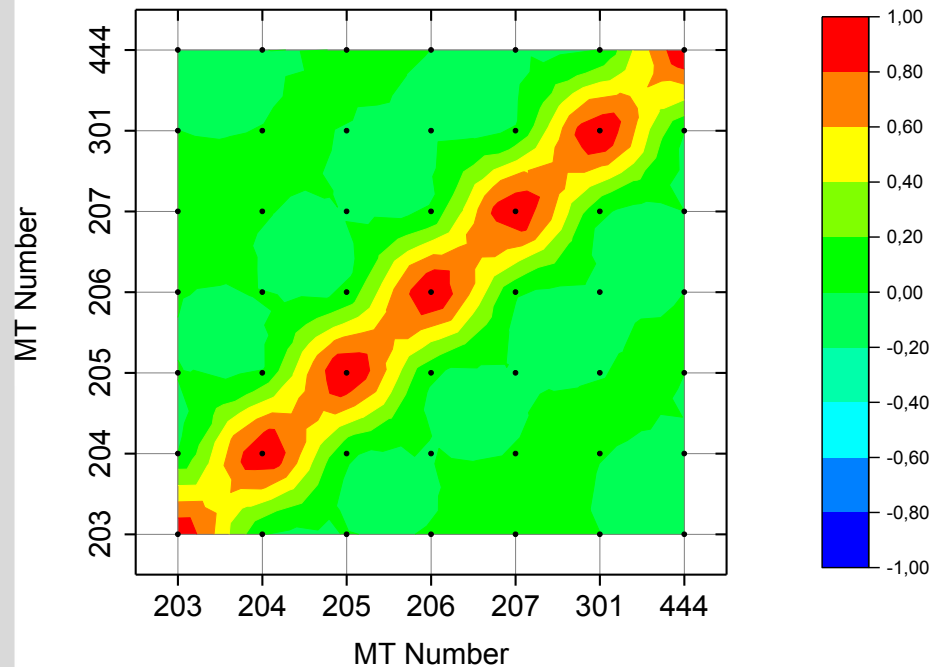
Findings:

- Nuclear Data Covariances result to 1.5 - 23% for SPA in Fission, Fusion and Spallation
- Neglecting E-E correlations reduces SPA Uncertainties by 2-3 times
- MT-MT correlations are small: for most practically important Cor (207,444) < 2 E-4

Practical Application: MT-MT Correlation Matrix for SPA Damage - results for MT=203-444

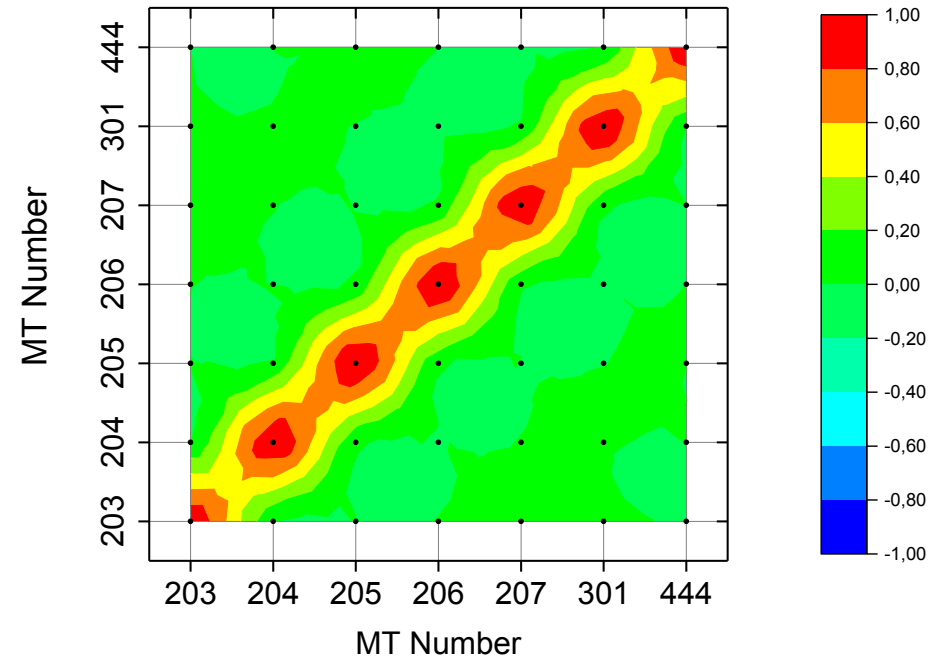
↓ MT-MT for HFIR/C5

Fe-56: MT-MT Correlation Matrix for SPA (HFIR/C5)
from 500 TENDL-2013 random files



↓ MT-MT for ITER/FW

Fe-56: MT-MT Correlation Matrix for SPA (ITER/FW)
from 500 TENDL-2013 random files



Findings: NO practically significant MT- MT correlations (Correlation $\leq 1\%$)

Practical Applications: Damage Uncertainties from Nuclear Data vs. Material Physics in representative Facilities



SPA Damage Uncertainties for ^{56}Fe in IFMIF/HFTM, ITER/FW and HFIR/C5

Source of Uncertainty:	Nuclear Data	Material Physics
Damage Energy DE	$\pm (1.4 - 3.1)\%$	
Lattice Thresh. $E_d = 40 \pm 2 \text{ eV}^*$		$\pm 5.0\%$
Sum Uncertainty for NRT-dpa $= 0.8 \cdot \text{DE} / 2E_d$	$\pm (5.2 - 5.9)\%$	
Defect Surviving Efficiency		OECD fit $\pm 2\%^{**}$ Spread MD $\sim \pm 20\%^{**}$
Sum Uncertainty for arc-dpa $\sim 0.8 \cdot \text{DE} / 2E_d \cdot \text{Efficiency}$	$\pm (5.2 - 5.9)\% + \pm (\approx 20)\%$	
KERMA \equiv local Nuclear Heating	$\pm (2.7 - 8.7)\%$	do not contribute
(n,xα) or (n,xH)	$\pm 23\%$ or $\pm 17\%$	do not contribute

*) K. Nordlund et al., NIM B246(2005)32

**) "Primary Radiation Damage in Materials", Report NEA/NSC/DOC(2015)9, OECD 2015

Findings: Material Physics parameters add 5% to NRT-dpa and 20% to arc-dpa

Summary

- E-E & MT-MT Covariance Matrices for Damage Quantities (Damage Energy, KERMA, Gas production) in ^{56}Fe were derived from TENDL-2013 random files
- E-E Covariance Matrices were written in ENDF-6 format as MF33 file, added to unperturbed evaluation and tested on positive definiteness and format compliance by standard checkers and NJOY
- for practical application (i.e. energy weighted quantities in representative fission, fusion or spallation facilities) the Uncertainty were (*first time ?*) estimated as:
 - 1.3-3.0% for NRT-dpa, 3-9 % for KERMA and 17-23% for Gas-production
- uncertainty for NRT/arc-dpa has to be additionally increased by 5/20% which stem from Material Physics
- Reaction-Reaction correlations found to be small: He-dpa < 2E-4, gas-gas < 1E-2